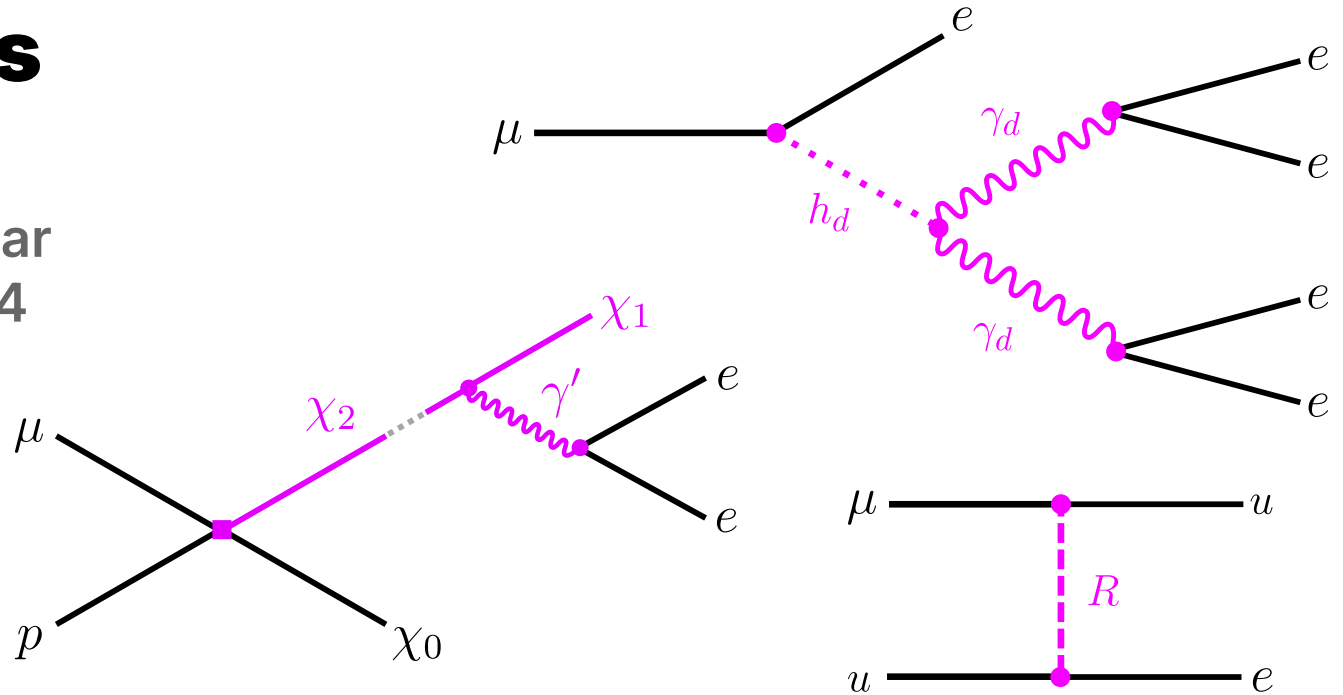


From heavy to light: new physics @ high-intensity μ experiments

Cornell University
LEPP Theory Seminar
November 13th, 2024

Tony Menzo
PhD candidate
University of Cincinnati



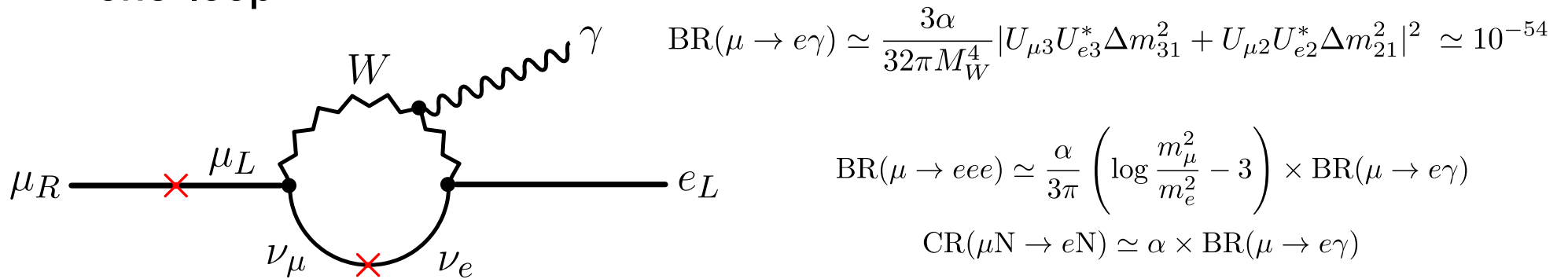
Based on [2306.15631](#), [2406.13818](#) and [2407.03450](#) with [Wick Haxton](#), [Ken McElvain](#), [Evan Rule](#), [Patrick Fox](#), [Matheus Hostert](#), [Maxim Pospelov](#), and [Jure Zupan](#)

$\mu \rightarrow e$

- The Standard Model (SM) has an accidental global flavor symmetry

$$U(1)_e \times U(1)_\mu \times U(1)_\tau$$

- Because $m_\nu \neq 0$ charged-lepton-flavor violation (CLFV) can occur at one-loop



Bottom line: Observing CLFV = new physics

Experimental status

- **Mu \rightarrow E Gamma (MEG) @ PSI - $\mu \rightarrow e\gamma$**

Projected: $\text{BR}(\mu^+ \rightarrow e^+ \gamma) \lesssim 6 \times 10^{-14}$ ($\Gamma(\mu \rightarrow e) \lesssim 10^{-10}$ Hz)

- **Mu3e @ PSI - $\mu \rightarrow eee$**

Projected: $\text{BR}(\mu^+ \rightarrow e^+ e^- e^+) \lesssim 10^{-16}$ ($\Gamma(\mu \rightarrow e) \lesssim 10^{-12}$ Hz)

- **Mu2e @ Fermilab, COMET @ J-PARC - $N\mu \rightarrow Ne$**

Projected: $\text{CR}(\mu^- \text{Al} \rightarrow e^- \text{Al}) \lesssim 10^{-18} - 10^{-17}$ ($\Gamma(\mu \rightarrow e) \lesssim 10^{-13}$ Hz)

Experimental status

- **Mu \rightarrow E Gamma**

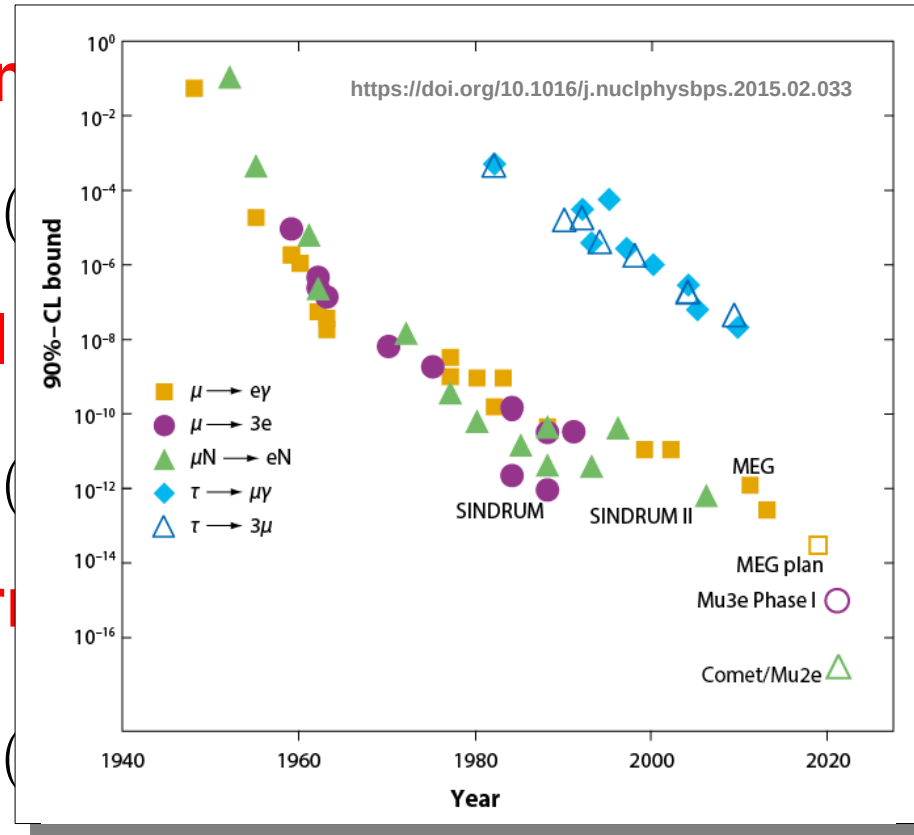
Projected: BR() $\lesssim 10^{-10}$ Hz)

- **Mu3e @ PSI**

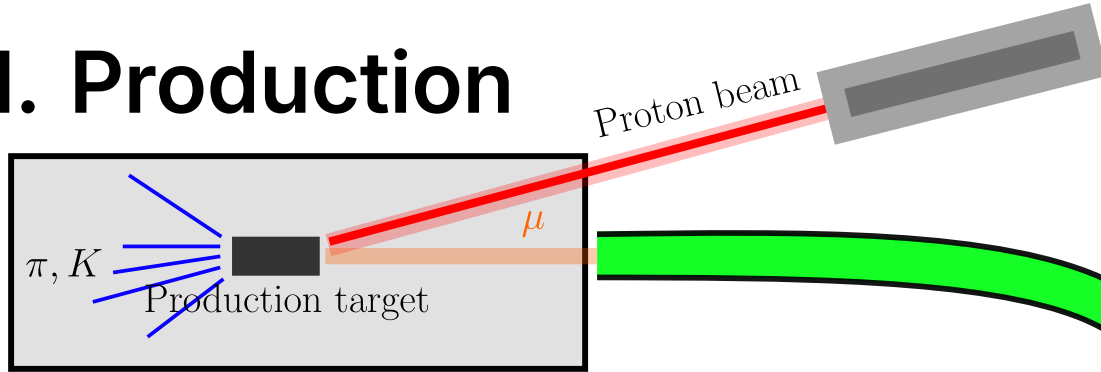
Projected: BR() $\lesssim 10^{-12}$ Hz)

- **Mu2e @ Fermilab**

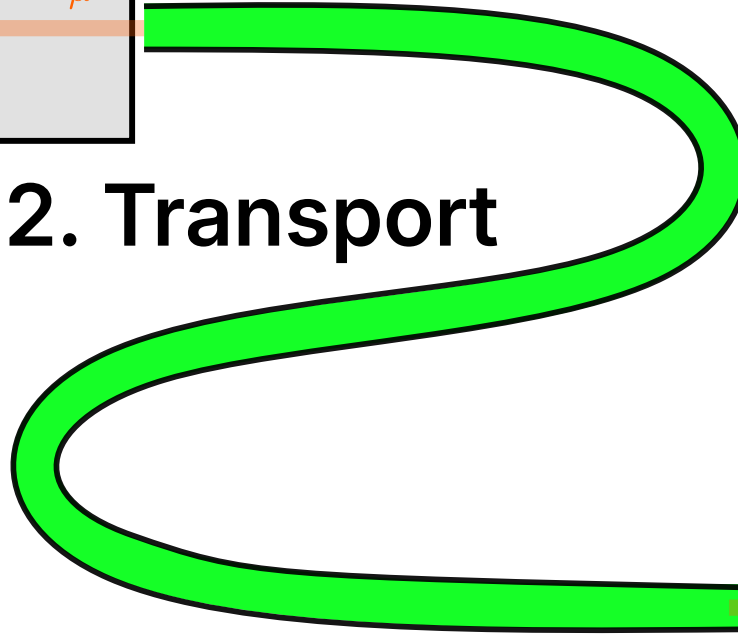
Projected: CR() $\Gamma(\mu \rightarrow e) \lesssim 10^{-13}$ Hz)



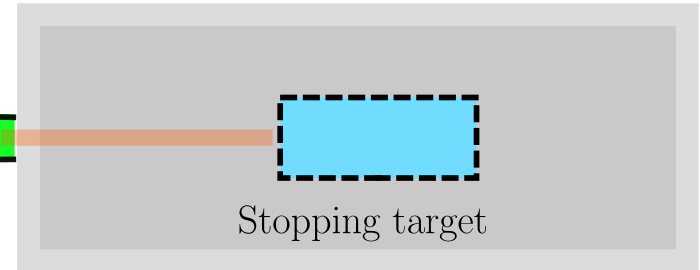
1. Production



2. Transport



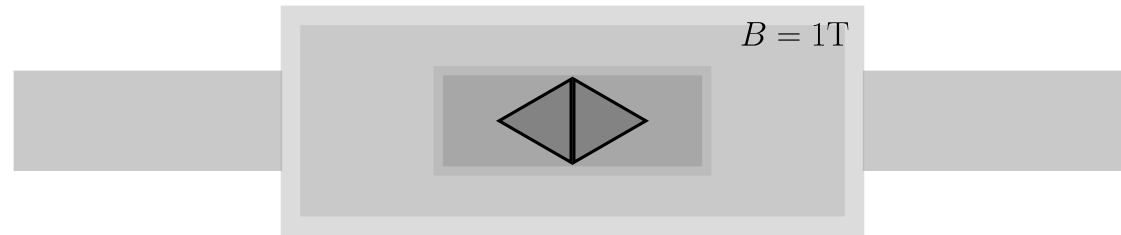
3. Stopping



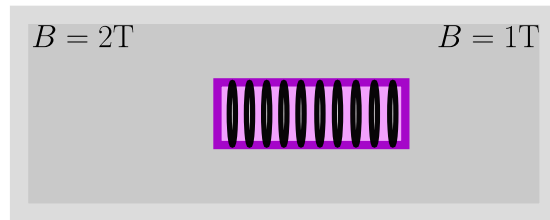
4. Detection (phenomenology is influenced by detector)

Mu3e (μ^+)

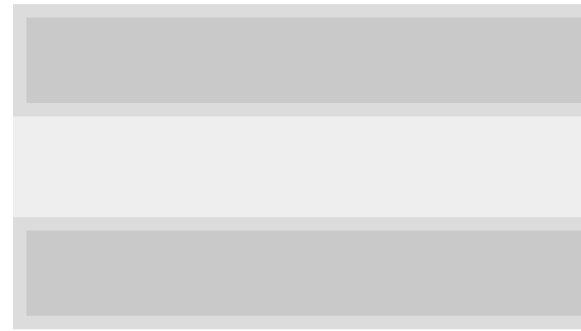
***requires $p_T > 10$ MeV**



Mu2e (μ^-)



***requires $p_T > 90$ MeV**



Exotic $\mu \rightarrow e$

In the *Landscape*, CLFV is common.

The dichotomy:

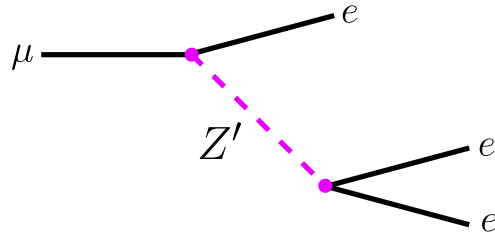
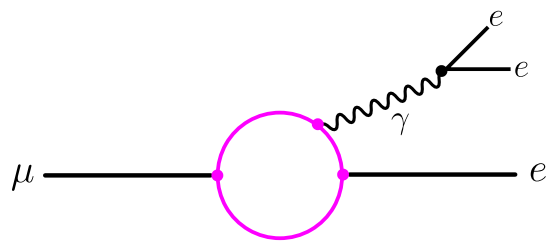
- Heavy: SM + "irrelevant" operators

- Light: SM + new fields with weakly coupled interactions

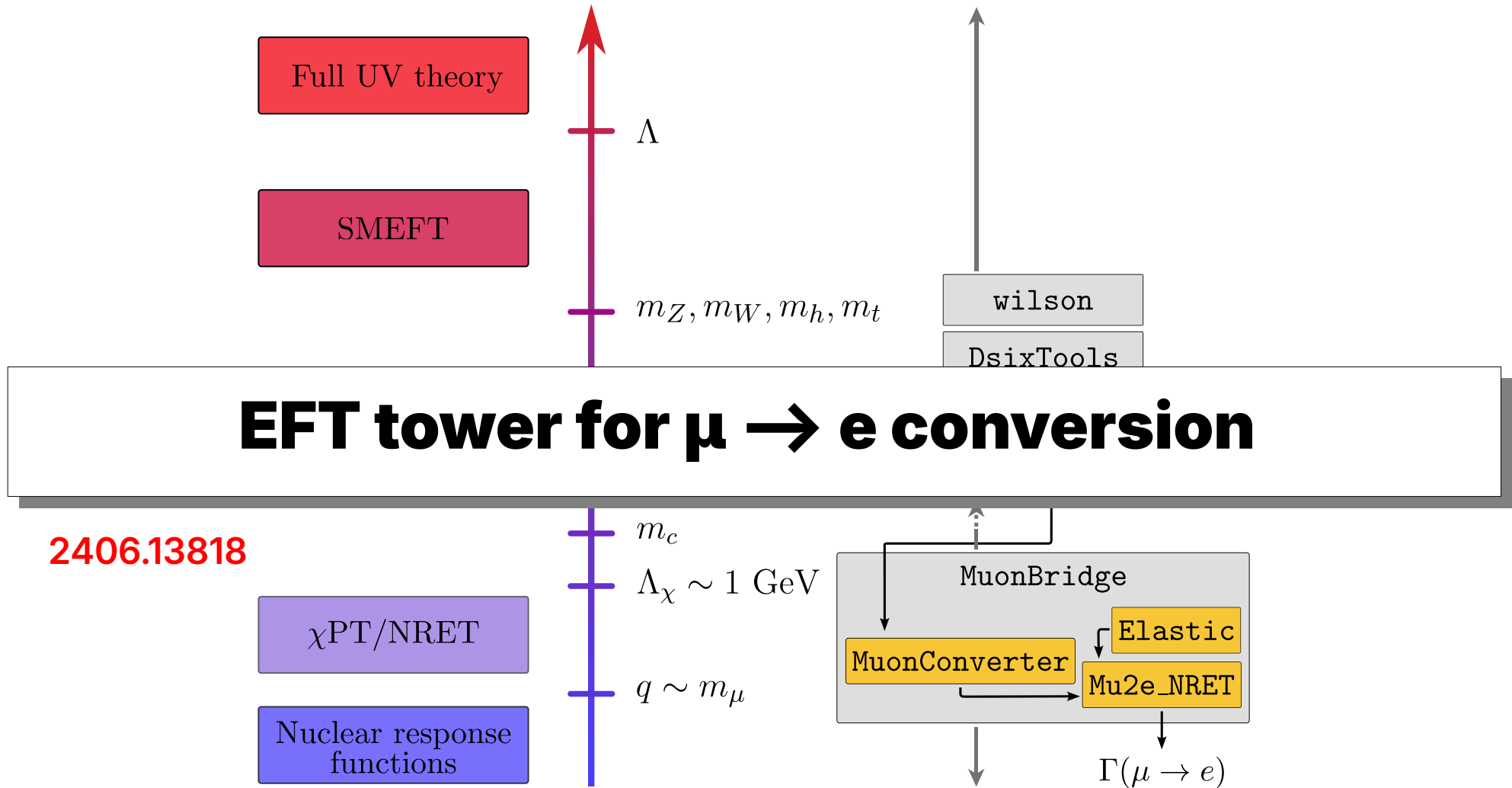
$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \sum_{d>4} \frac{1}{\Lambda^{d-4}} O^{(d)}$$

- "Photonic" – e.g. SUSY, massive neutrinos, ...

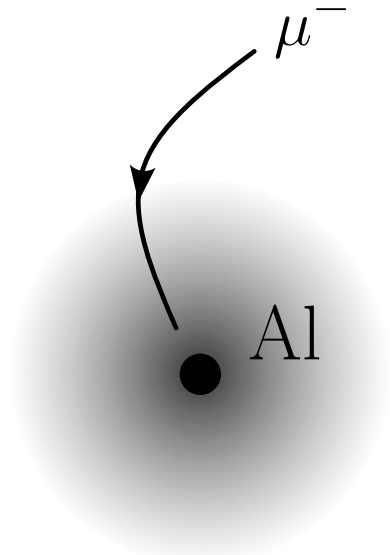
- "Contact" – e.g. Z' , leptoquarks, ...



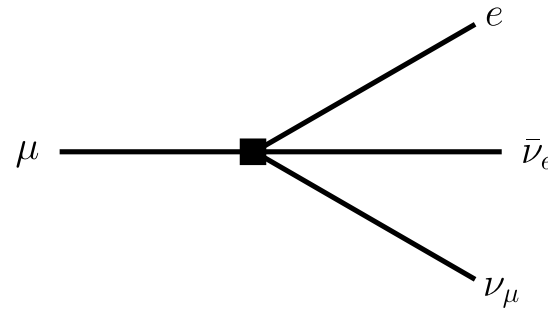
*Naturalness demands an explanation! Appeal to high scale physics to explain smallness



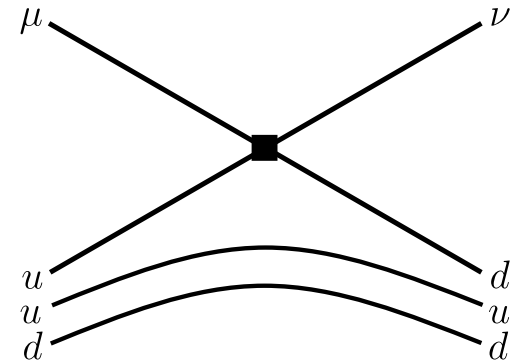
A trapped muon can...



1. **Decay in orbit**



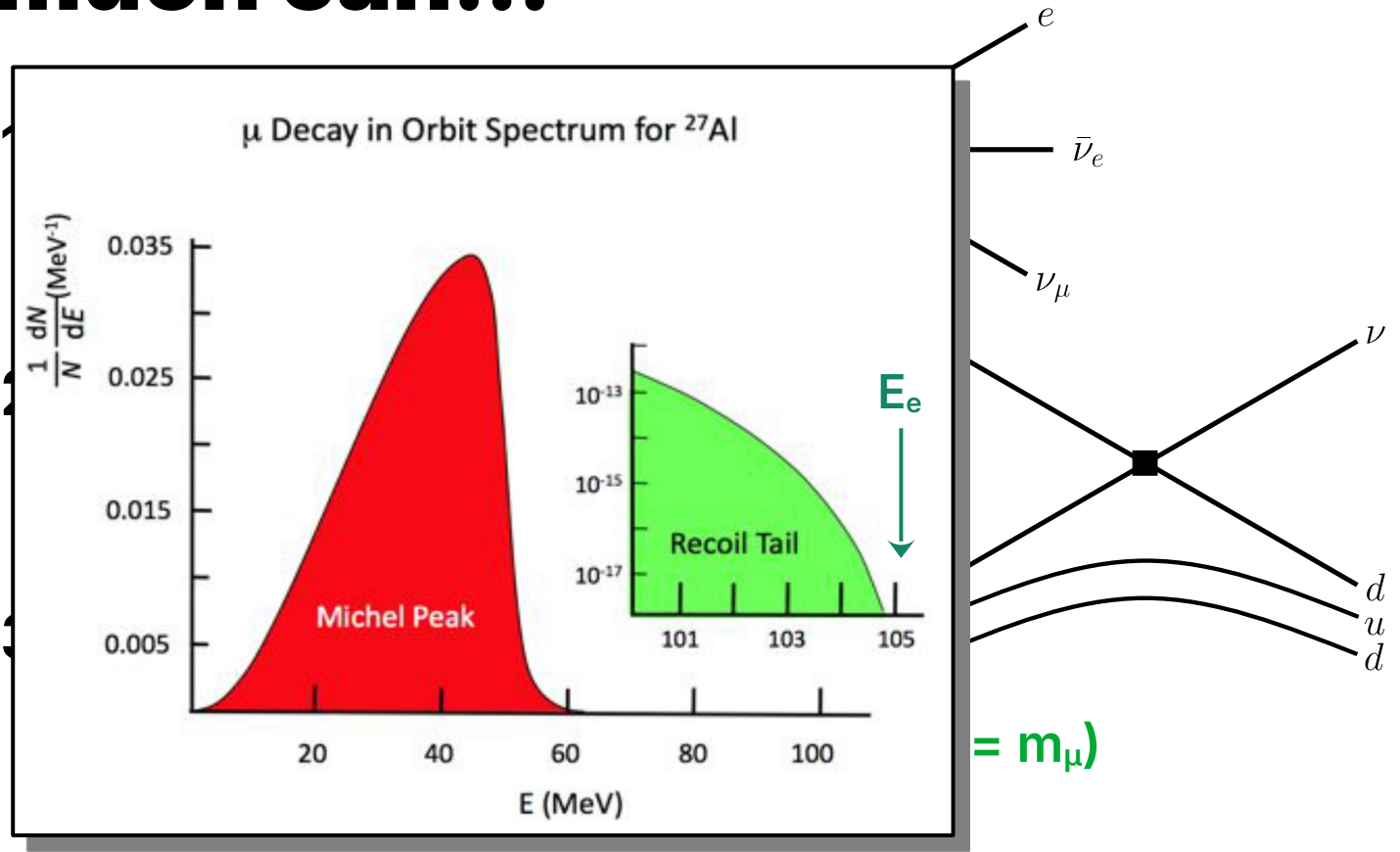
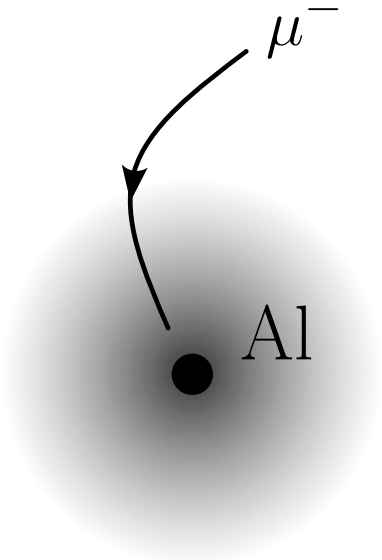
2. **Be captured by the nucleus**



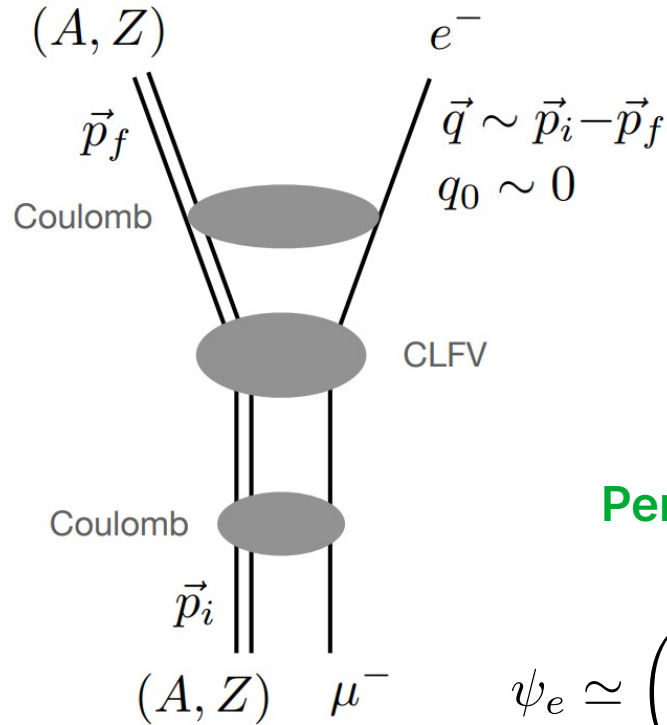
3. **Convert to an electron**

a) **Mono-energetic electron signal ($E_e = m_\mu$)**

A trapped muon can...



$(A, Z) \mu^- \rightarrow (A, Z) e^-$



Schematically...

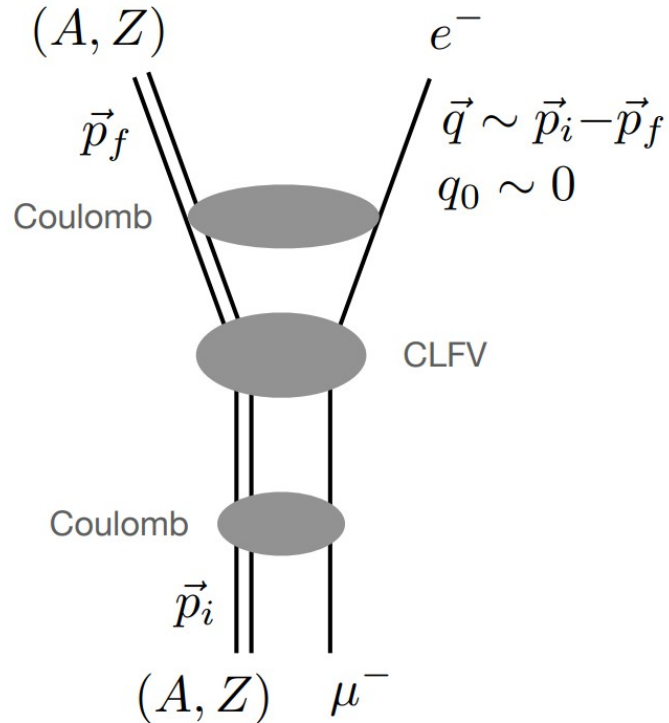
- Effective Hamiltonian:

$$\mathcal{H}_i = c_i \int d^3x \bar{\psi}_e(\vec{x}) O_L \psi_\mu(\vec{x}) \bar{\psi}_N(\vec{x}) O_N \psi_N(\vec{x})$$

Perform partial-wave and multipole expansion...

$$\psi_e \simeq \begin{pmatrix} \xi \\ \hat{q} \cdot \vec{\sigma} \xi \end{pmatrix} \quad \psi_\mu \simeq \begin{pmatrix} \xi \\ \frac{1}{2} \vec{v}_\mu \cdot \vec{\sigma} \xi \end{pmatrix} \quad \psi_N \simeq \begin{pmatrix} \xi \\ \frac{1}{2} \vec{v}_N \cdot \vec{\sigma} \xi \end{pmatrix}$$

$(A, Z) \mu^- \rightarrow (A, Z) e^-$



At the end of the day:

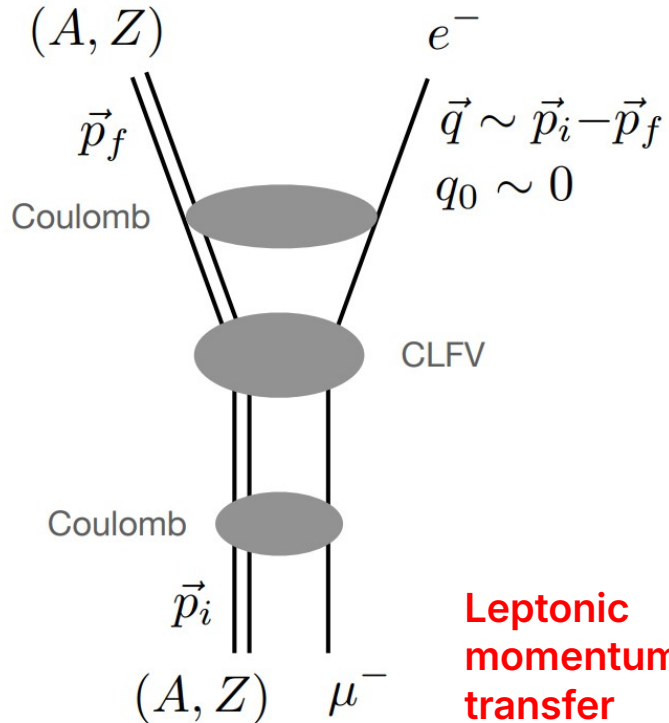
- Basis of CLFV'ing single-nucleon operators

$$i\hat{q} = \frac{i\vec{q}}{|\vec{q}|}, \quad \vec{\sigma}_L, \quad \vec{\sigma}_N, \quad \vec{v}_N, \quad \vec{v}_\mu.$$

- Natural hierarchy of dimensionless scales

$$y \equiv \left(\frac{qb}{2} \right)^2 > |\vec{v}_N| > |\vec{v}_\mu| > |\vec{v}_T|$$

$(A, Z) \mu^- \rightarrow (A, Z) e^-$



At the end of the day:

- Basis of CLFV'ing single-nucleon operators

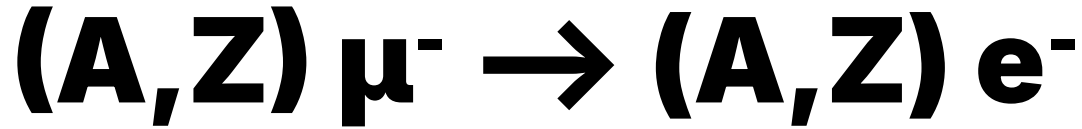
$$i\hat{q} = \frac{i\vec{q}}{|\vec{q}|}, \quad \vec{\sigma}_L, \quad \vec{\sigma}_N, \quad \vec{v}_N, \quad \vec{v}_\mu.$$

- Natural hierarchy of dimensionless scales

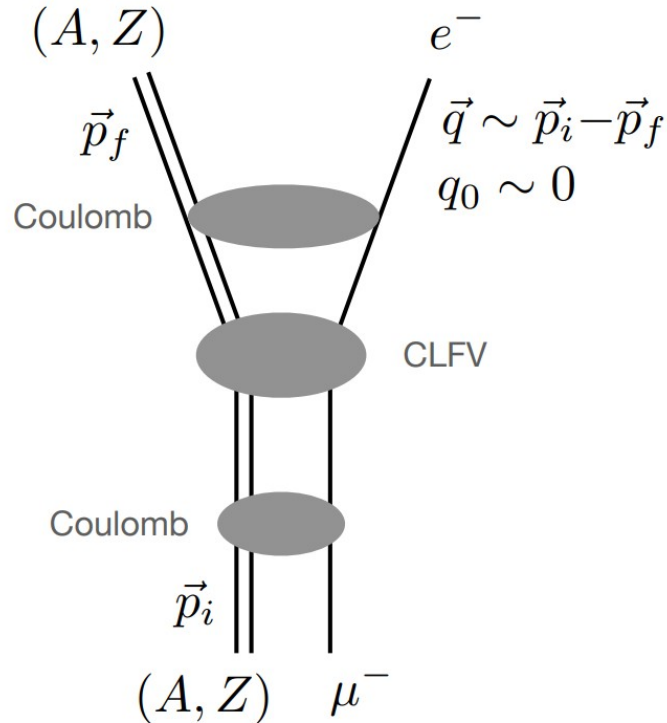
$$y \equiv \left(\frac{qb}{2} \right)^2 \approx 0.25 > |\vec{v}_N| \approx 0.2 > |\vec{v}_\mu| > |\vec{v}_T|$$

$q \approx m_\mu = 1/1.86 \text{ fm}$ $b = 1.85 \text{ fm}$

^{27}Al Harmonic oscillator parameter



2208.07945



Nuclear-level Effective Theory of $\mu \rightarrow e$ Conversion:
Formalism and Applications

W. C. Haxton,^{1,2} Evan Rule,¹ Ken McElvain,¹ and Michael J. Ramsey-Musolf^{3,4}

¹Department of Physics, University of California, Berkeley, California 94720, USA

²Lawrence Berkeley National Laboratory, Berkeley, California 94720, USA

³Tsung-Dao Lee Institute and School of Physics and Astronomy, Shanghai Jiao Tong University, 800 Dongchuan Road, Shanghai 200240, China

⁴Amherst Center for Fundamental Interactions, Department of Physics, University of Massachusetts, Amherst, Massachusetts 01003, USA

(Dated: April 4, 2023)

Over the next decade new $\mu \rightarrow e$ conversion searches at Fermilab (Mu2e) and J-PARC (COMET, DeeMe) are expected to advance limits on charged lepton flavor violation (CLFV) by more than four orders of magnitude. By considering the consequence of P and CP on elastic $\mu \rightarrow e$ conversion and the structure of possible charge and current densities, we show that rates are governed by six nuclear responses and a single scale, q/m_N , where $q \approx m_\mu$ is the momentum transferred from the leptons to the nucleus. To relate this result to microscopic formulations of CLFV, we construct in nonrelativistic effective theory (NRET) the CLFV nucleon-level interaction, pointing out the relevance of the dimensionless scales $y = (\frac{q}{m_N})^2 > |\vec{v}_N| > |\vec{v}_\mu| > |\vec{v}_T|$, where b is the nuclear size, \vec{v}_N and \vec{v}_μ are the nucleon and muon intrinsic velocities, and \vec{v}_T is the target recoil velocity. We discuss previous work, noting the lack of a systematic treatment of the various small parameters. Because the parameter y is not small, a proper calculation of $\mu \rightarrow e$ conversion requires a full multipole expansion of the nuclear response functions, an apparently daunting task with Coulomb-distorted electron partial waves. We demonstrate that the multipole expansion can be carried out to high precision by introducing a simplifying local momentum q_{eff} for the electron. Previous work has been limited to simple charge or spin interactions, thereby treating the nucleus effectively as a point particle. We show that such formulations are not compatible with the general form of the $\mu \rightarrow e$ conversion rate, failing to generate three of the six allowed nuclear response functions. The inclusion of the nucleon velocity \vec{v}_N yields an NRET with 16 operators and a rate of the general form. Consequently, in the current discovery era for CLFV, it provides the most sensible starting point for experimental analysis, defining what can and cannot be determined about CLFV from the highly exclusive process of $\mu \rightarrow e$ conversion. Finally, we expand the NRET operator basis to account for the effects of \vec{v}_μ , associated with the muon's lower component, generating corrections to the CLFV coefficients of the point-nucleus response functions. Using advanced shell-model methods, we compute $\mu \rightarrow e$ conversion rates for a series of experimental targets, deriving bounds on the coefficients of the CLFV operators. These calculations are the first to include a general basis of CLFV operators, full evaluation of the associated nuclear response functions, and an accurate treatment of electron and muon Coulomb effects. We discuss target selection as an experimental "knob" that can be turned to probe the microscopic origins of CLFV. We describe two types of coherence that enhance certain CLFV operators and selection rules that blind elastic $\mu \rightarrow e$ conversion to others. We discuss the matching of the NRET onto higher level effective field theories, such as those constructed at the light quark level, noting opportunities to build on existing work in direct detection of dark matter. We discuss the relation of $\mu \rightarrow e$ conversion to $\mu \rightarrow e + \gamma$ and $\mu \rightarrow 3e$, showing how MEG II and Mu3e results will complement those of Mu2e and COMET. Finally we describe a accompanying script - in Mathematica and Python versions - that can be used to compute $\mu \rightarrow e$ conversion rates in various nuclear targets for the full set of NRET operators.

I. INTRODUCTION

Muon-to-electron conversion, in which a muon bound to a nucleus converts to a mono-energetic outgoing electron, occurs at an observable level only if there are new sources of flavor violation, beyond those responsible for neutrino mixing [1–4]. It has

yond the standard model [5–7]. This has motivated a series of experimental advances that, in sum, have improved limits on $\mu \rightarrow e$ conversion rates by ≈ 12 orders of magnitude over the past 75 years [8].

The experimental attributes of $\mu \rightarrow e$ conversion are quite attractive. Intense muon beams exist, with rates on target of $\approx 10^{11}/\text{s}$ expected in the

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The rate

- The conversion rate: $\mathcal{O}(y)$

$$\Gamma(\mu \rightarrow e) = \frac{1}{2\pi} \frac{q_{\text{eff}}^2}{1 + q/M_T} |\phi_{1s}^{Z_{\text{eff}}}(\vec{0})|^2 \sum_{\tau, \tau'} \left[R_{MM}^{\tau\tau'} W_{MM}^{\tau\tau'}(q_{\text{eff}}) \right. \\ \left. + R_{\Sigma'\Sigma'}^{\tau\tau'} W_{\Sigma'\Sigma'}^{\tau\tau'}(q_{\text{eff}}) + R_{\Sigma''\Sigma''}^{\tau\tau'} W_{\Sigma''\Sigma''}^{\tau\tau'}(q_{\text{eff}}) \right],$$

$$R_{MM}^{\tau\tau'} = c_1^\tau c_1^{\tau'*} + c_{11}^\tau c_{11}^{\tau'*},$$

$$R_{\Sigma'\Sigma'}^{\tau\tau'} = c_4^\tau c_4^{\tau'*} + c_9^\tau c_9^{\tau'*},$$

$$R_{\Sigma''\Sigma''}^{\tau\tau'} = (c_4^\tau - c_6^\tau)(c_4^{\tau'} - c_6^{\tau'})^* + c_{10}^\tau c_{10}^{\tau'*},$$

The rate

- The conversion rate: $\mathcal{O}(\vec{v}_N)$ ***All nuclear responses allowed by symmetries are generated**

$$\omega = \frac{G_F^2}{\pi} \frac{q_{\text{eff}}^2}{1 + \frac{q}{M_T}} |\phi_{1s}^{Z_{\text{eff}}}(\vec{0})|^2 \sum_{\tau=0,1} \sum_{\tau'=0,1} \left\{ \begin{aligned} & \left[\tilde{R}_{MM}^{\tau\tau'} W_{MM}^{\tau\tau'}(q_{\text{eff}}) + \tilde{R}_{\Sigma''\Sigma''}^{\tau\tau'} W_{\Sigma''\Sigma''}^{\tau\tau'}(q_{\text{eff}}) + \tilde{R}_{\Sigma'\Sigma'}^{\tau\tau'} W_{\Sigma'\Sigma'}^{\tau\tau'}(q_{\text{eff}}) \right] \\ & + \frac{q_{\text{eff}}^2}{m_N^2} \left[\tilde{R}_{\Phi''\Phi''}^{\tau\tau'} W_{\Phi''\Phi''}^{\tau\tau'}(q_{\text{eff}}) + \tilde{R}_{\tilde{\Phi}\tilde{\Phi}}^{\tau\tau'} W_{\tilde{\Phi}\tilde{\Phi}}^{\tau\tau'}(q_{\text{eff}}) + \tilde{R}_{\Delta\Delta}^{\tau\tau'} W_{\Delta\Delta}^{\tau\tau'}(q_{\text{eff}}) \right] \\ & - \frac{2q_{\text{eff}}}{m_N} \left[\tilde{R}_{\Phi''M}^{\tau\tau'} W_{\Phi''M}^{\tau\tau'}(q_{\text{eff}}) + \tilde{R}_{\Delta\Sigma'}^{\tau\tau'} W_{\Delta\Sigma'}^{\tau\tau'}(q_{\text{eff}}) \right] \end{aligned} \right\} \quad (59)$$

$$R_{MM}^{\tau\tau'} = c_1^\tau c_1^{\tau'*} + c_{11}^\tau c_{11}^{\tau'*},$$

$$R_{\Sigma'\Sigma'}^{\tau\tau'} = c_4^\tau c_4^{\tau'*} + c_9^\tau c_9^{\tau'*},$$

$$R_{\Sigma''\Sigma''}^{\tau\tau'} = (c_4^\tau - c_6^\tau)(c_4^{\tau'} - c_6^{\tau'})^* + c_{10}^\tau c_{10}^{\tau'*},$$

$$\tilde{R}_{\Phi''\Phi''}^{\tau\tau'} = \tilde{c}_3^\tau \tilde{c}_3^{\tau'*} + (\tilde{c}_{12}^\tau - \tilde{c}_{15}^\tau)(\tilde{c}_{12}^{\tau'*} - \tilde{c}_{15}^{\tau'*})$$

$$\tilde{R}_{\Phi''M}^{\tau\tau'} = \text{Re}[\tilde{c}_3^\tau \tilde{c}_1^{\tau'*} - (\tilde{c}_{12}^\tau - \tilde{c}_{15}^\tau) \tilde{c}_{11}^{\tau'*}]$$

$$\tilde{R}_{\Delta\Delta}^{\tau\tau'} = \tilde{c}_5^\tau \tilde{c}_5^{\tau'*} + \tilde{c}_8^\tau \tilde{c}_8^{\tau'*}$$

$$\tilde{R}_{\Delta\Sigma'}^{\tau\tau'} = \text{Re}[\tilde{c}_5^\tau \tilde{c}_4^{\tau'*} + \tilde{c}_8^\tau \tilde{c}_9^{\tau'*}]$$

$$\tilde{R}_{\tilde{\Phi}\tilde{\Phi}}^{\tau\tau'} = \tilde{c}_{12}^\tau \tilde{c}_{12}^{\tau'*} + \tilde{c}_{13}^\tau \tilde{c}_{13}^{\tau'*}$$

Nuclear response hierarchy

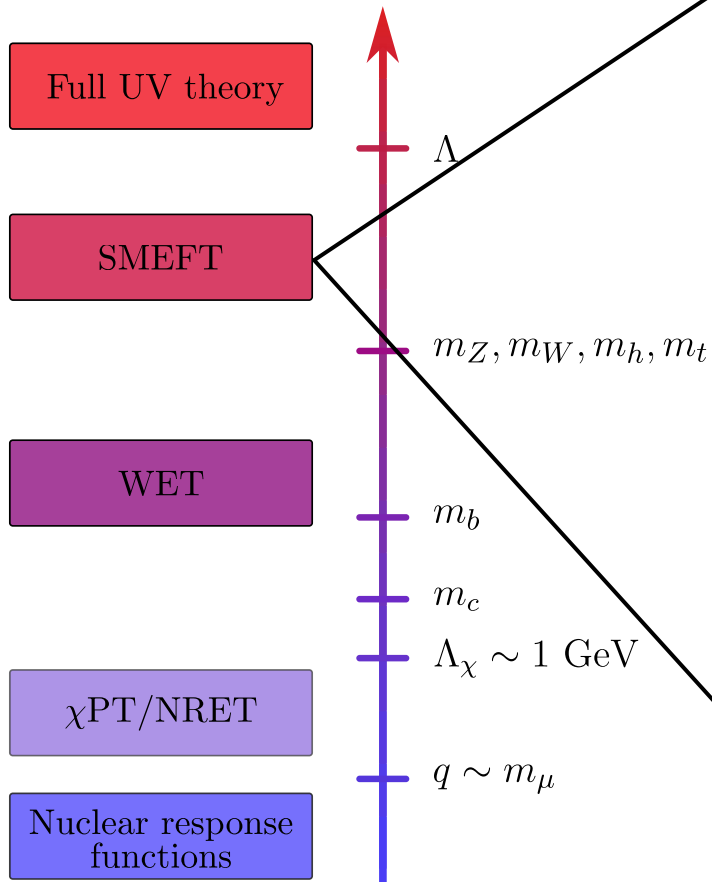
*Can become semi-coherent in some nuclei with half-filled shells (e.g. Al, Cu)

$$W_{MM}^{00} \sim \mathcal{O}(A^2) \gg \frac{q_{\text{eff}}}{m_N} W_{M\Phi''}^{00} \gg \left\{ W_{\Sigma'\Sigma'}^{00}, W_{\Sigma''\Sigma''}^{00}, \frac{q_{\text{eff}}^2}{m_N^2} W_{\Phi''\Phi''}^{00} \right\} \gg \left\{ \frac{q_{\text{eff}}^2}{m_N^2} W_{\Delta\Delta}^{00}, \frac{q_{\text{eff}}^2}{m_N^2} W_{\tilde{\Phi}'\tilde{\Phi}'}^{00} \right\}$$

Where does the UV physics sit?

$$\Gamma \propto \sum R \times W, \quad R(c_i)$$

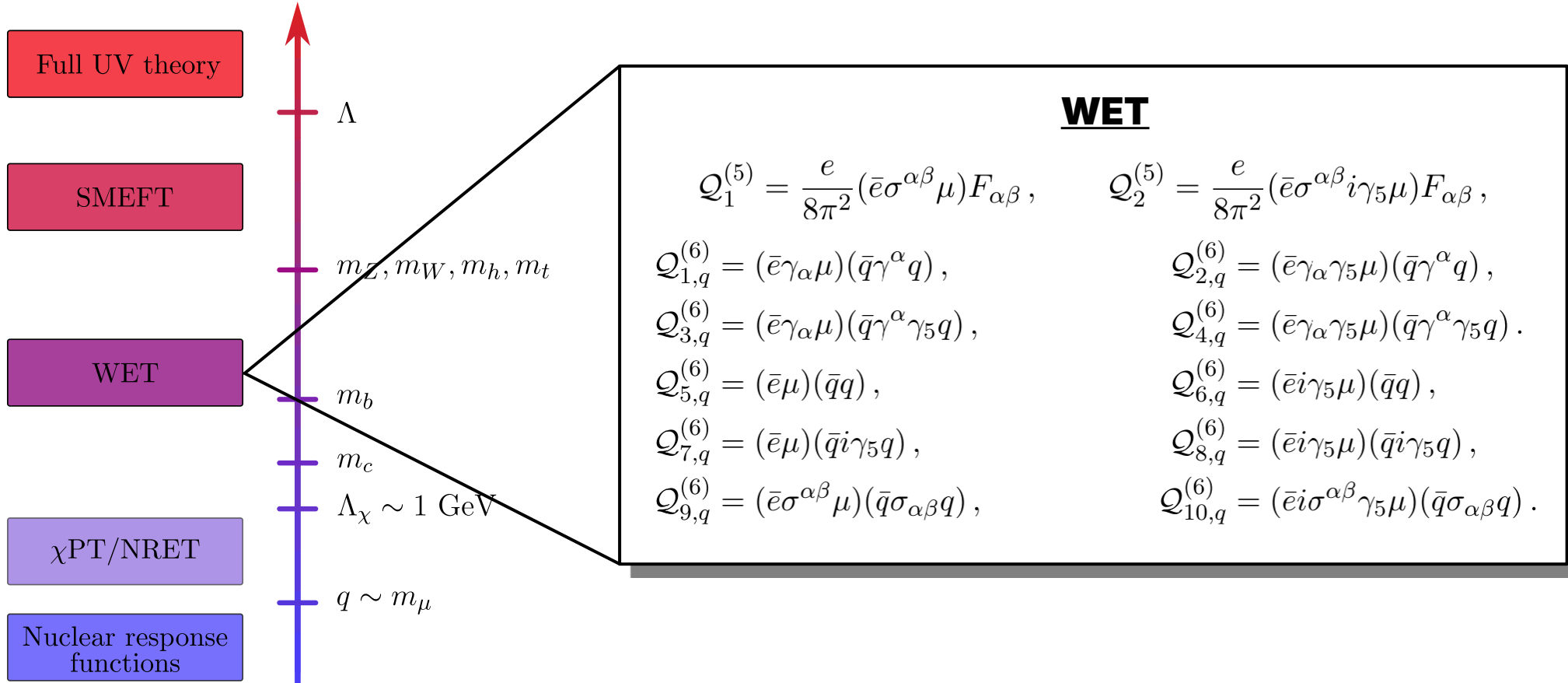
The tower



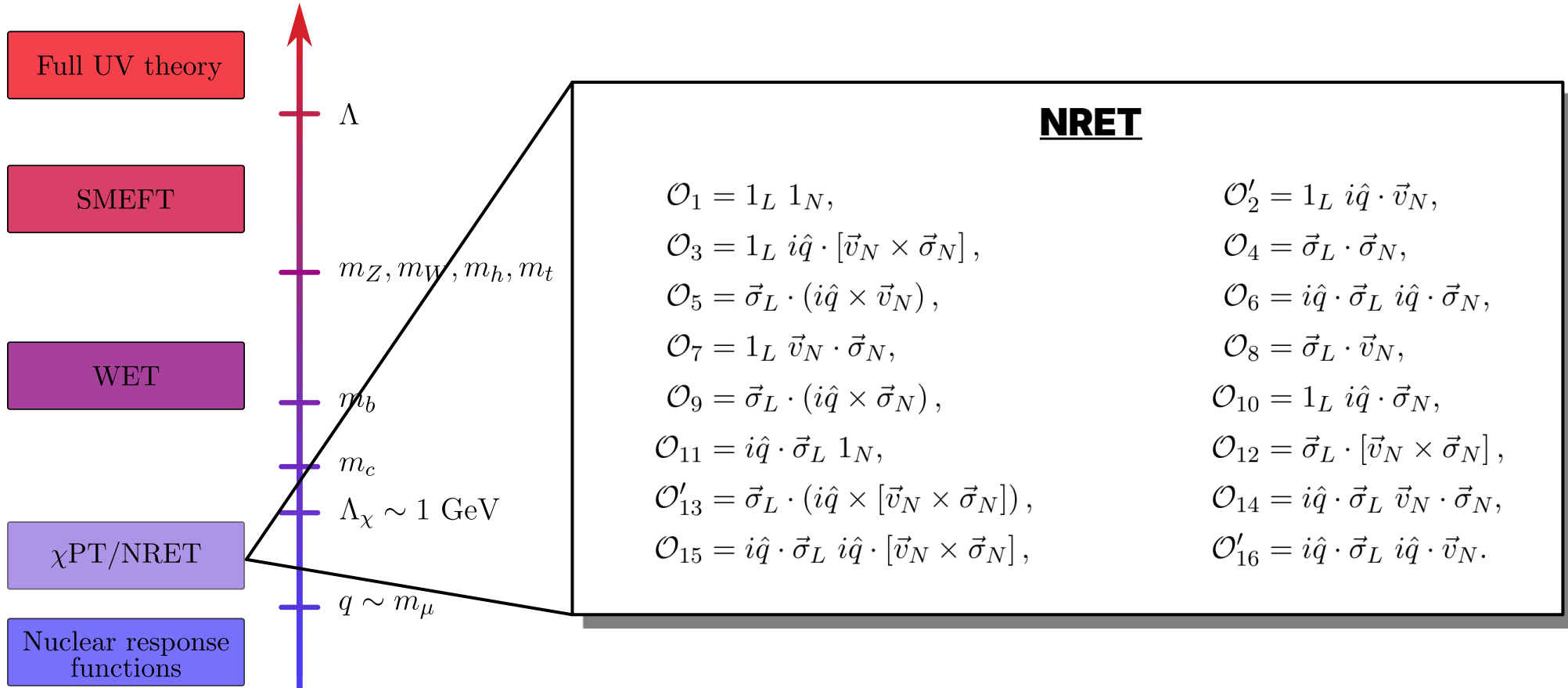
SMEFT

$$\begin{aligned}
 Q_{e\varphi} &: (\varphi^\dagger \varphi) (\bar{L}_2 e_R \varphi), \quad (\varphi^\dagger \varphi) (\bar{l}_1 \mu_R \varphi), \\
 Q_{eW} &: (\bar{l}_2 \sigma^{\mu\nu} e_R) \tau^I \varphi W_{\mu\nu}^I, \quad (\bar{l}_1 \sigma^{\mu\nu} \mu_R) \tau^I \varphi W_{\mu\nu}^I, \\
 Q_{eB} &: (\bar{l}_2 \sigma^{\mu\nu} e_R) \varphi B_{\mu\nu}, \quad (\bar{l}_1 \sigma^{\mu\nu} \mu_R) \varphi B_{\mu\nu}, \\
 Q_{\varphi l}^{(1)} &: (\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi) (\bar{l}_2 \gamma^\mu l_1), \\
 Q_{\varphi l}^{(3)} &: (\varphi^\dagger i \overleftrightarrow{D}_\mu^I \varphi) (\bar{l}_2 \gamma^\mu \tau^I l_1), \\
 Q_{\varphi e} &: (\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi) (\bar{\mu}_R \gamma^\mu \tau^I e_R), \\
 Q_{lq}^{(1)} &: (\bar{l}_2 \gamma^\mu l_1) (\bar{q} \gamma^\mu q), \\
 Q_{lq}^{(3)} &: (\bar{l}_2 \gamma^\mu \tau^I l_1) (\bar{q} \gamma^\mu \tau^I q), \\
 Q_{eu} &: (\bar{\mu}_R \gamma^\mu e_R) (\bar{u}_R \gamma^\mu u_R), \\
 Q_{ed} &: (\bar{\mu}_R \gamma^\mu e_R) (\bar{d}_R \gamma^\mu d_R), \\
 Q_{lu} &: (\bar{l}_2 \gamma^\mu l_1) (\bar{u}_R \gamma^\mu u_R), \\
 Q_{ld} &: (\bar{l}_2 \gamma^\mu l_1) (\bar{d}_R \gamma^\mu d_R), \\
 Q_{qe} &: (\bar{q} \gamma^\mu q) (\bar{\mu}_R \gamma^\mu e_R), \\
 Q_{ledq} &: (\bar{l}_2 e_R) (\bar{d}_R q), \quad (\bar{l}_1 \mu_R) (\bar{d}_R q), \\
 Q_{lequ}^{(1)} &: (\bar{l}_2^j e_R) \varepsilon_{jk} (\bar{q}^k u), \quad (\bar{l}_1^j \mu_R) \varepsilon_{jk} (\bar{q}^k u), \\
 Q_{lequ}^{(3)} &: (\bar{l}_2^j \sigma_{\mu\nu} e_R) \varepsilon_{jk} (\bar{q}^k \sigma^{\mu\nu} u), \quad (\bar{l}_1^j \sigma_{\mu\nu} \mu_R) \varepsilon_{jk} (\bar{q}^k \sigma^{\mu\nu} u),
 \end{aligned}$$

The tower



The tower



Matching

- Non-perturbative matching between WET and NRET (hadronization)
- Parameterize with nuclear form factors

$$\langle N' | \bar{q} \gamma^\mu q | N \rangle = \bar{u}'_N \left[F_1^{q/N}(q^2) \gamma^\mu - \frac{i}{2m_N} F_2^{q/N}(q^2) \sigma^{\mu\nu} q_\nu \right] u_N,$$

$$\langle N' | \bar{q} \gamma^\mu \gamma_5 q | N \rangle = \bar{u}'_N \left[F_A^{q/N}(q^2) \gamma^\mu \gamma_5 - \frac{1}{2m_N} F_{P'}^{q/N}(q^2) \gamma_5 q^\mu \right] u_N,$$

$$\langle N' | m_q \bar{q} q | N \rangle = F_S^{q/N}(q^2) \bar{u}'_N u_N,$$

$$\langle N' | m_q \bar{q} i \gamma_5 q | N \rangle = F_P^{q/N}(q^2) \bar{u}'_N i \gamma_5 u_N,$$

$$\langle N' | \frac{\alpha_s}{12\pi} G^{a\mu\nu} G_{\mu\nu}^a | N \rangle = F_G^N(q^2) \bar{u}'_N u_N,$$

$$\langle N' | \frac{\alpha_s}{8\pi} G^{a\mu\nu} \tilde{G}_{\mu\nu}^a | N \rangle = F_{\tilde{G}}^N(q^2) \bar{u}'_N i \gamma_5 u_N,$$

$$\langle N' | \bar{q} \sigma^{\mu\nu} q | N \rangle = \bar{u}'_N \left[\hat{F}_{T,0}^{q/N}(q^2) \sigma^{\mu\nu} - \frac{i}{2m_N} \gamma^{[\mu} q^{\nu]} \hat{F}_{T,1}^{q/N}(q^2) - \frac{i}{m_N^2} q^{[\mu} k_{12}^{\nu]} \hat{F}_{T,2}^{q/N}(q^2) \right] u_N,$$

$$\langle N' | \frac{\alpha}{12\pi} F^{\mu\nu} F_{\mu\nu} | N \rangle = F_\gamma^N(q^2) \bar{u}'_N u_N,$$

$$\langle N' | \frac{\alpha}{8\pi} F^{\mu\nu} \tilde{F}_{\mu\nu} | N \rangle = F_{\tilde{\gamma}}^N(q^2) \bar{u}'_N i \gamma_5 u_N.$$

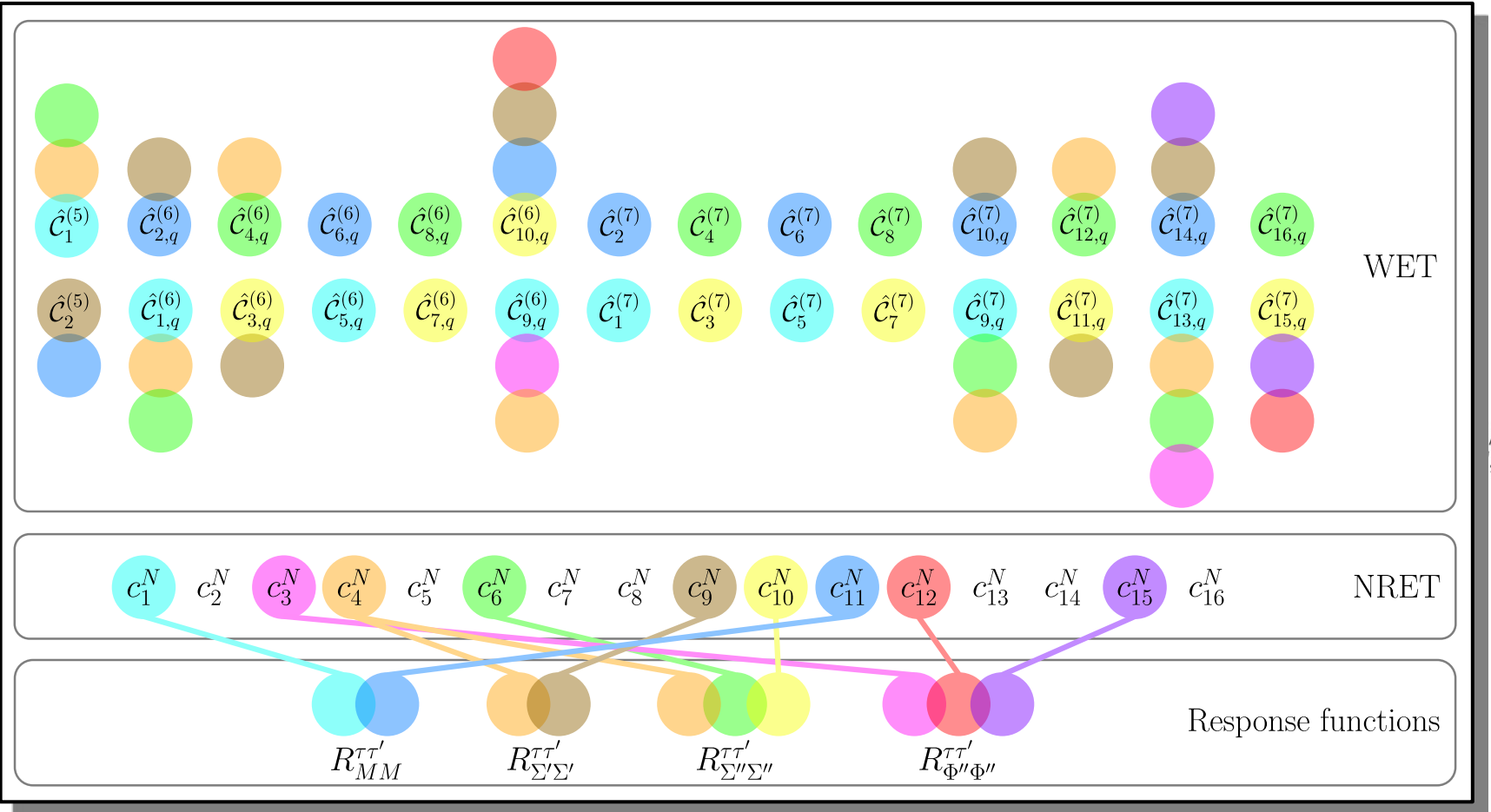
EFT tower

- Non-perturbative matching between WET and NRET (hadronization)
- Matching expressions

$$\begin{aligned}
 c_1^N &= -\frac{\alpha}{\pi q} \hat{C}_1^{(5)} \sum_q Q_q F_1^{q/N} + \sum_q \hat{C}_{1,q}^{(6)} F_1^{q/N} + \sum_q \frac{1}{m_q} \hat{C}_{5,q}^{(6)} F_S^{q/N} \\
 &\quad - \frac{q}{m_N} \sum_q \hat{C}_{9,q}^{(6)} (\hat{F}_{T,0}^{q/N} - \hat{F}_{T,1}^{q/N} + 4\hat{F}_{T,2}^{q/N}) \\
 &\quad + \hat{C}_1^{(7)} F_G^N + \hat{C}_5^{(7)} F_\gamma^N + (q + m_+) \sum_q \hat{C}_{9,q}^{(7)} F_1^{q/N} \\
 &\quad - \frac{q^2}{2m_N} \sum_q \hat{C}_{13,q}^{(7)} \left[\hat{F}_{T,0}^{q/N} - \hat{F}_{T,1}^{q/N} + \left(4 + \frac{q^2}{m_N^2} \right) \hat{F}_{T,2}^{q/N} \right], \\
 c_2^N &= i \left[\sum_q \hat{C}_{1,q}^{(6)} F_1^{q/N} + m_+ \sum_q \hat{C}_{9,q}^{(7)} F_1^{q/N} + \frac{q^2}{2m_N} \sum_q \hat{C}_{13,q}^{(7)} (\hat{F}_{T,1}^{q/N} - 4\hat{F}_{T,2}^{q/N}) \right], \\
 &\quad \vdots
 \end{aligned}$$

EF

- No ma
- Ma ex



$\left. \begin{matrix} /N \\ ,2 \end{matrix} \right) \Bigg]$

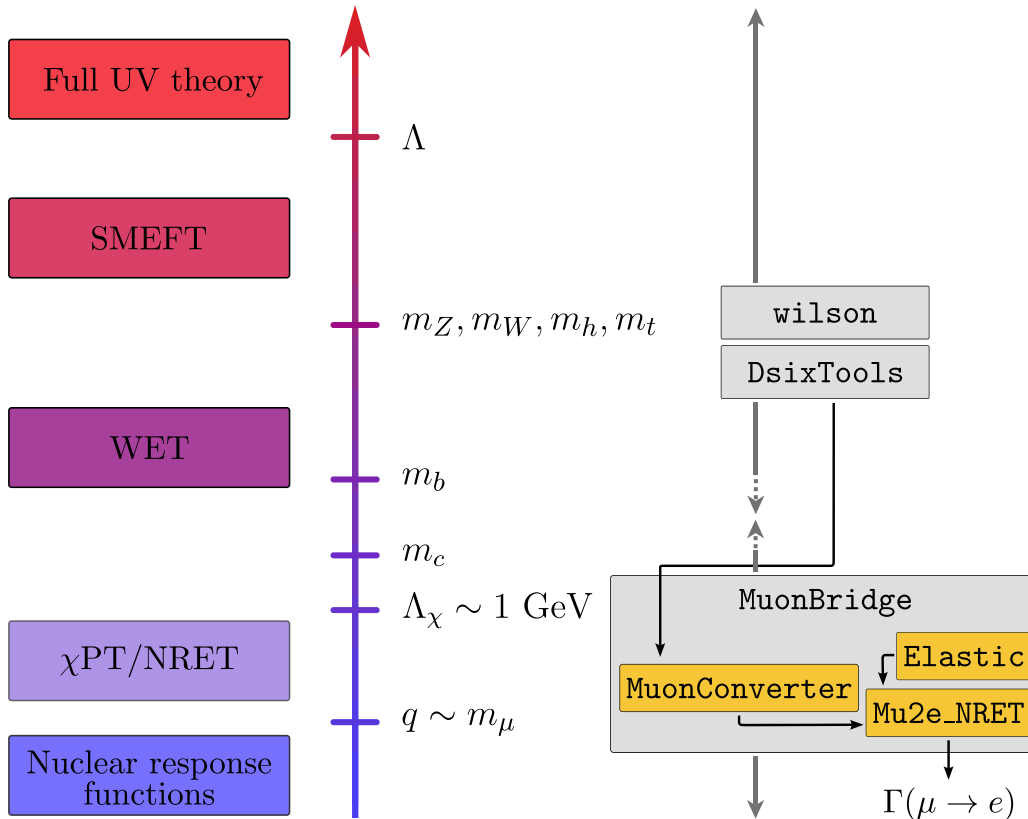
MuonBridge

<https://github.com/Berkeley-Electroweak-Physics/MuonBridge>



Three components:

1. Elastic - one body density matrices
2. Mu2e_NRET - Computes $\mu \rightarrow e$ conversion rate
3. MuonConverter - matches WET to NRET and facilitates interface with existing EFT software



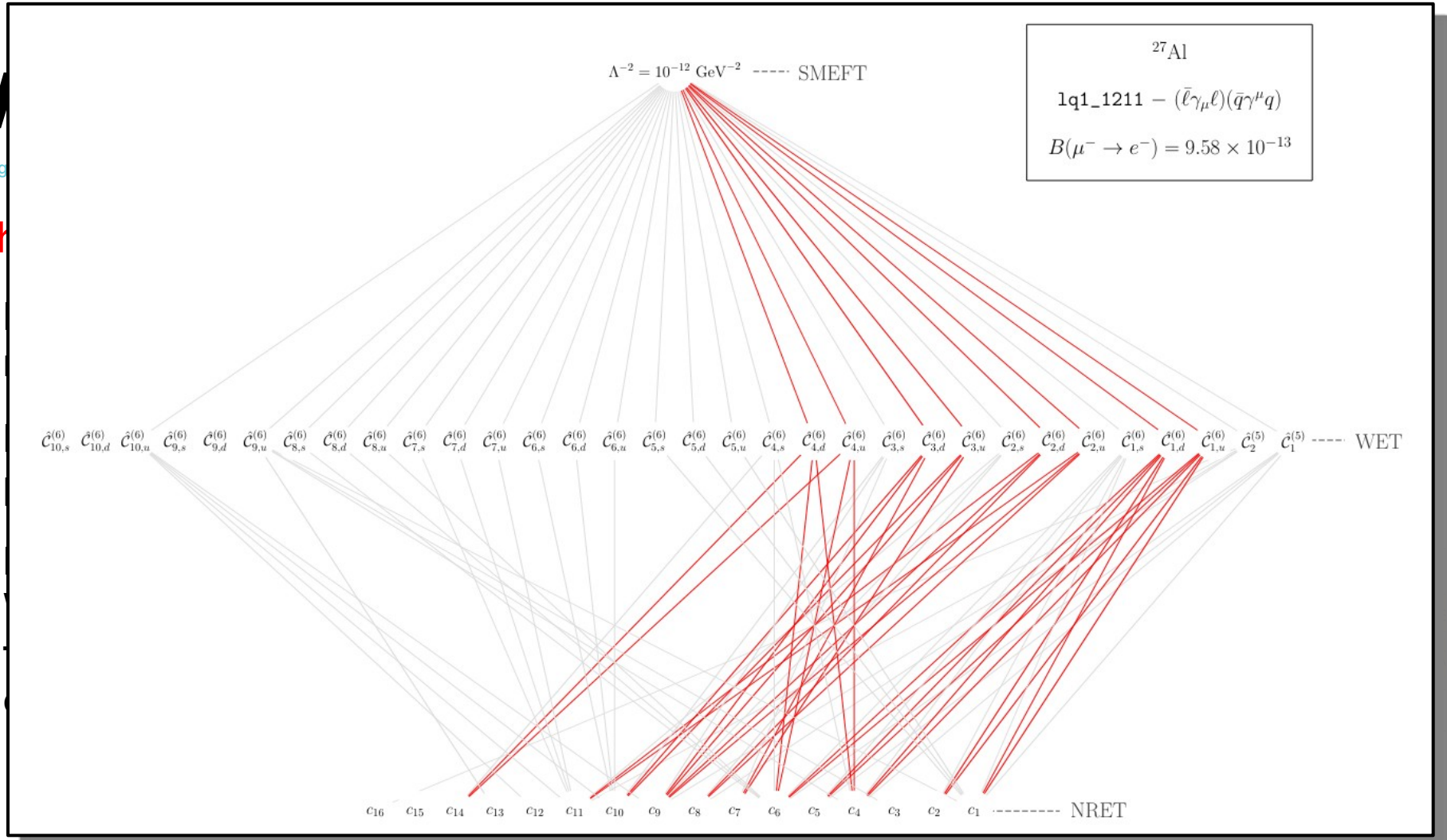
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1.

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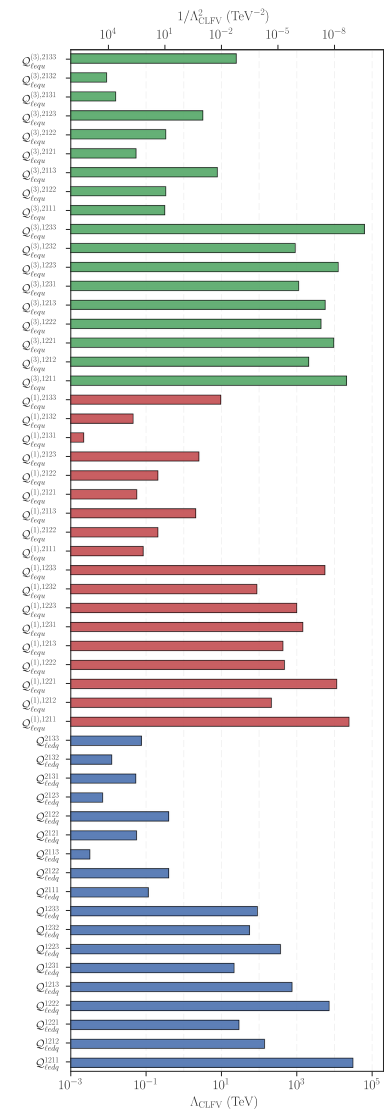
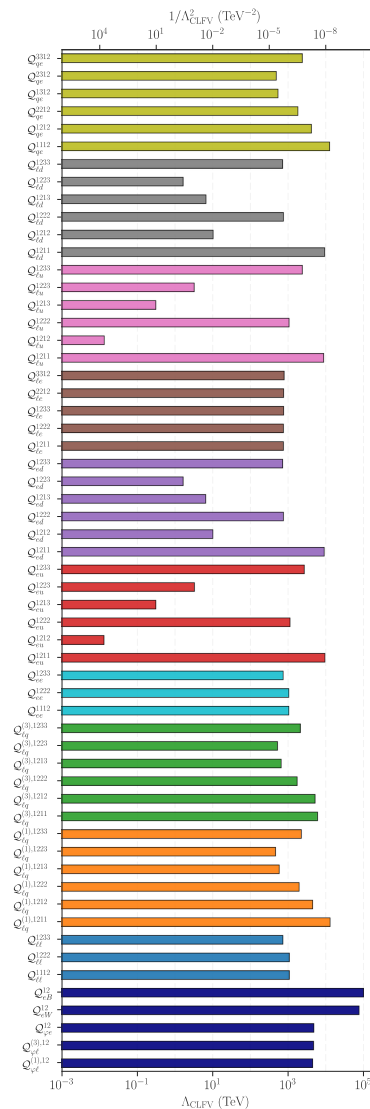
tic

RET

$\rightarrow e)$

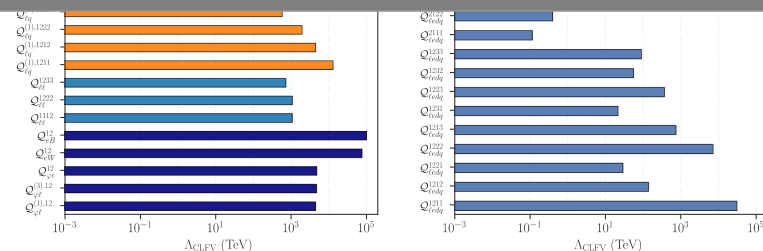
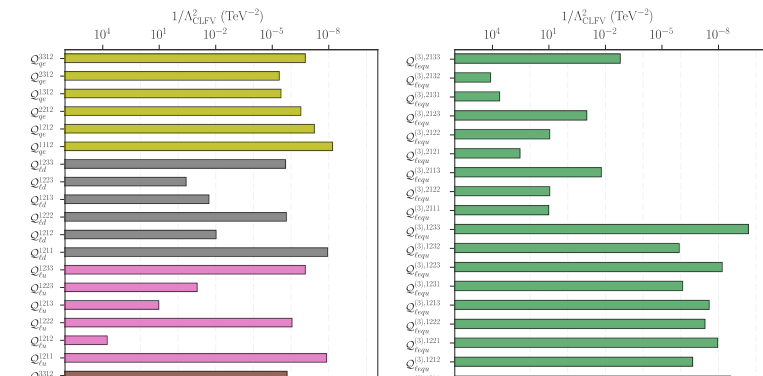
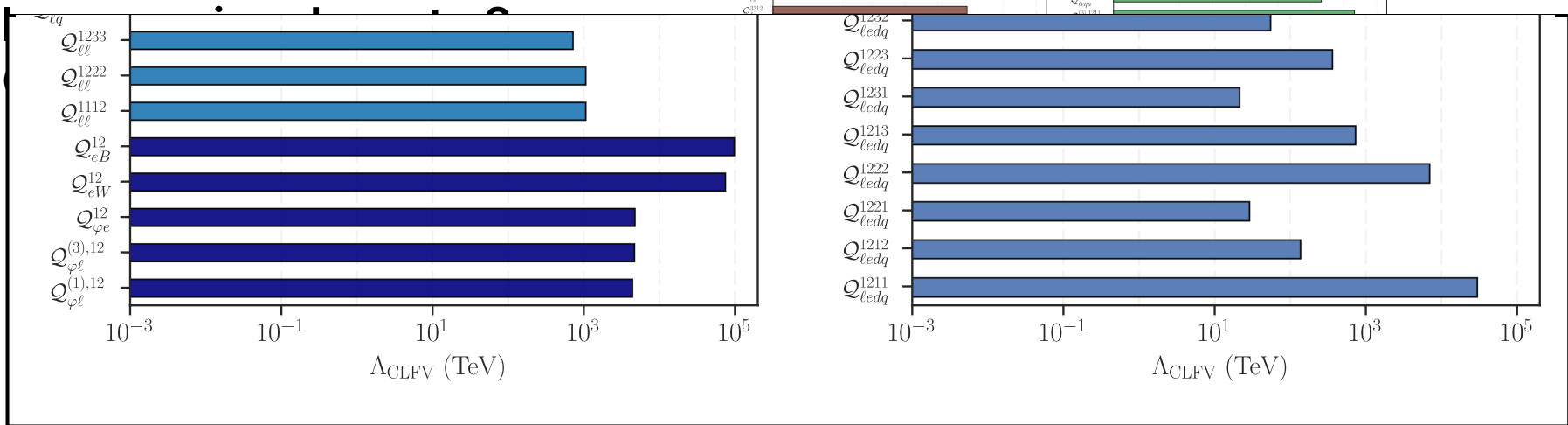
Bottom-up

- Single dim-6 SMEFT operator bounds (with one-loop running down to 2 GeV)



Bottom-up

- Single dim-6 SMEFT operator bounds (with one-



Top-down

- Consider the following leptoquark model

$$\mathcal{L} \supset -y_{2ij}^{RL} \bar{u}_R^i R_2^a \epsilon^{ab} L_L^{j,b} + y_{2ij}^{LR} \bar{e}_R^i R_2^{a*} Q_L^{j,a} + \text{h.c.},$$

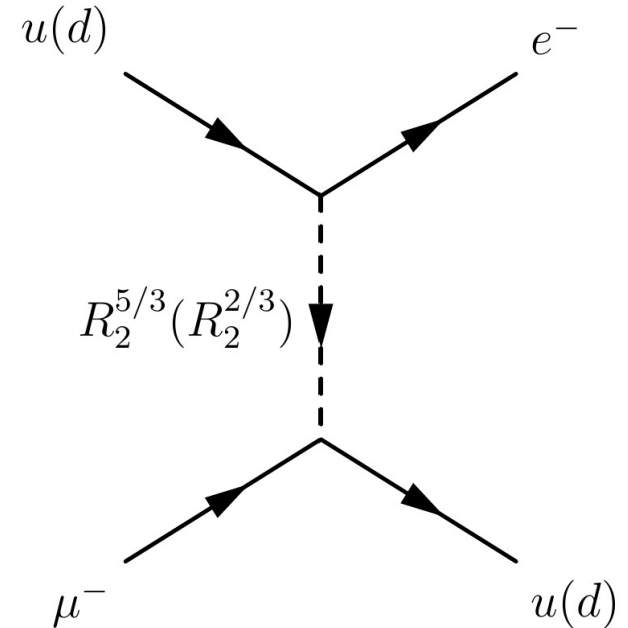
Match onto SMEFT @ $\Lambda = m_{LQ}$:

$$C_{12ii}^{lu} = -\frac{1}{2m_{LQ}^2} y_{2i2}^{RL} y_{2i1}^{RL*},$$

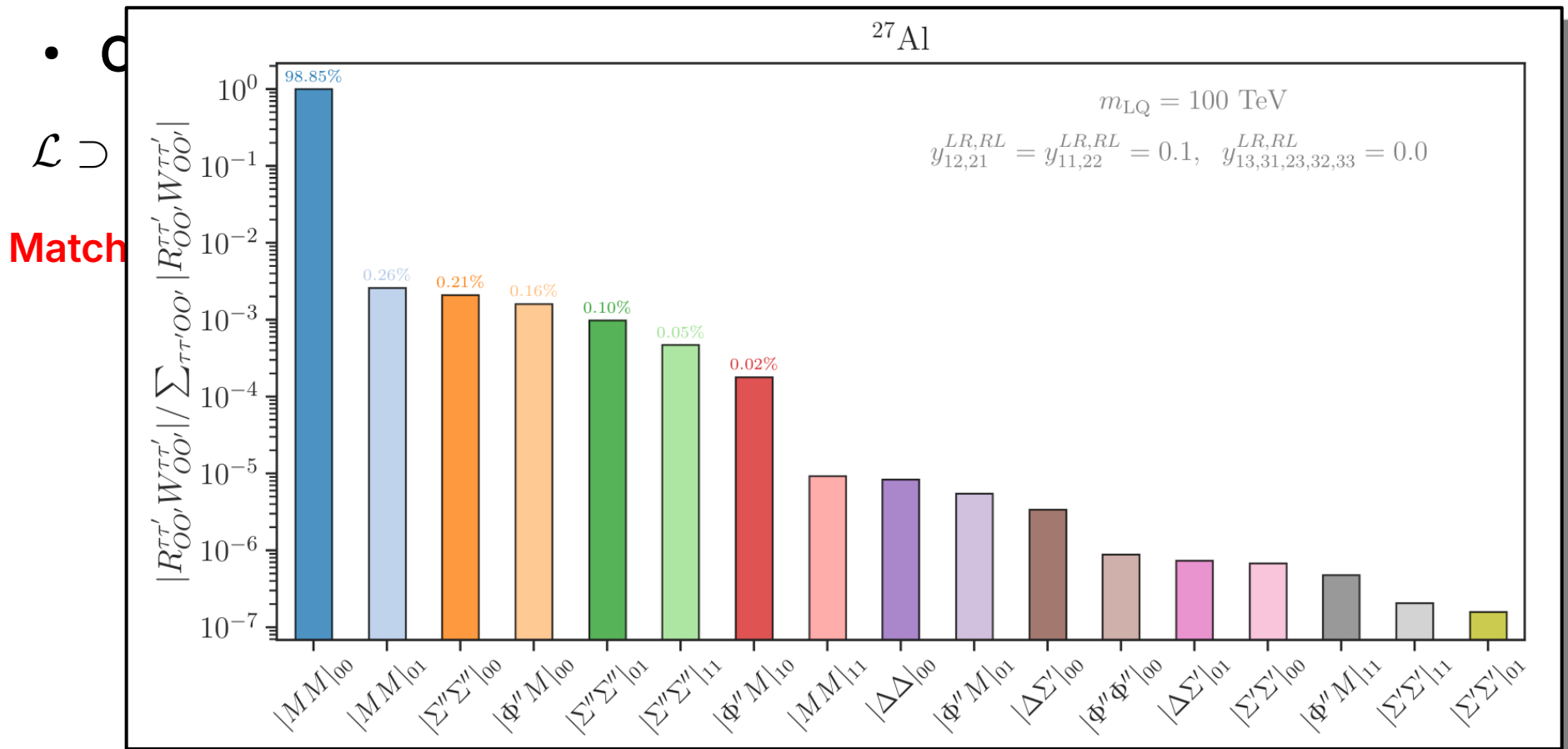
$$C_{ii12}^{qe} = -\frac{1}{2m_{LQ}^2} y_{22i}^{LR*} y_{21i}^{LR},$$

$$C_{12ii}^{(1)lequ} = 2C_{12ii}^{(3)lequ} = -\frac{1}{2m_{LQ}^2} y_{22i}^{LR*} y_{2i1}^{RL*},$$

$$C_{21ii}^{(1)lequ*} = 2C_{21ii}^{(3)lequ*} = -\frac{1}{2m_{LQ}^2} y_{2i2}^{LR} y_{21i}^{RL},$$



Top-down

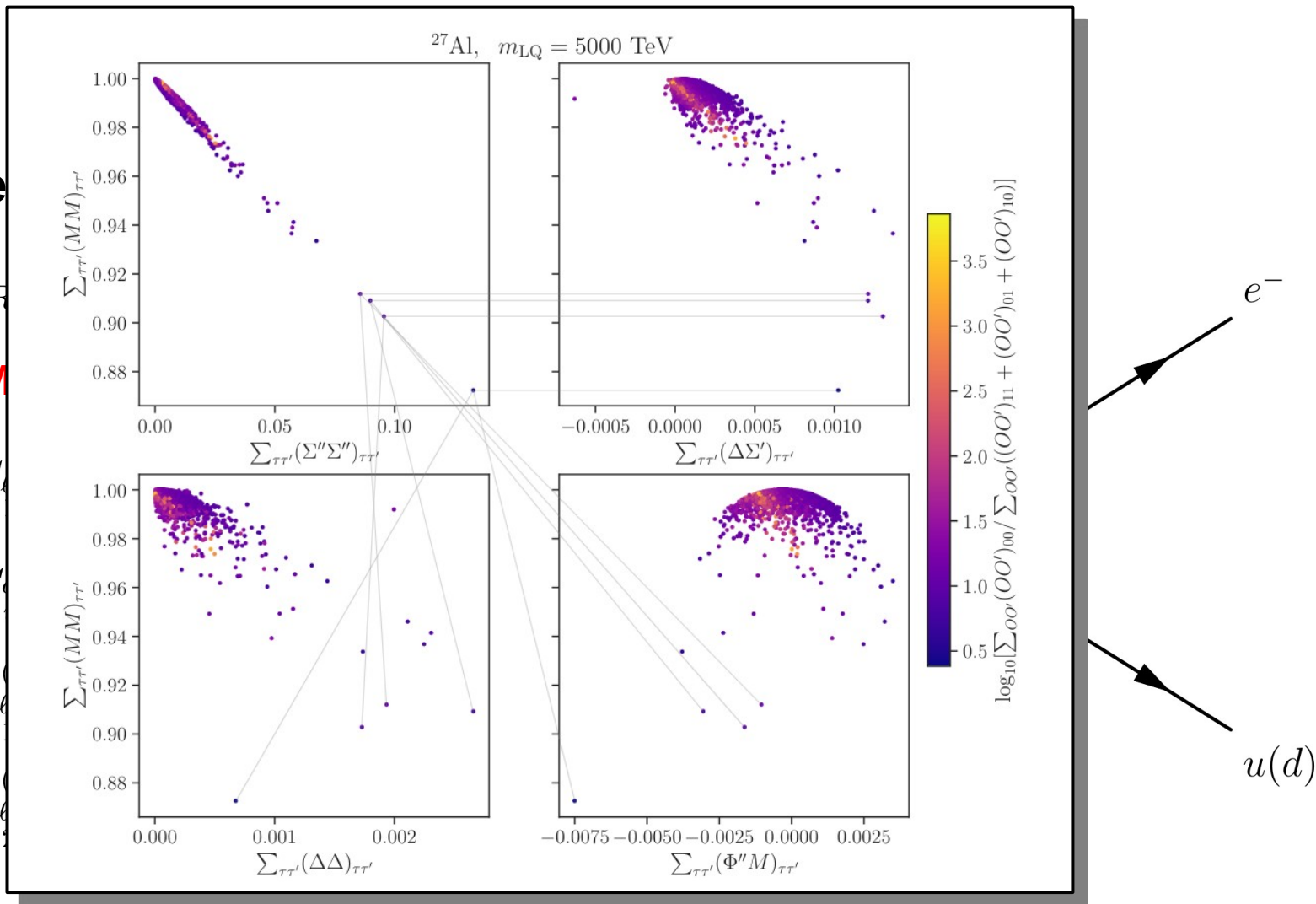


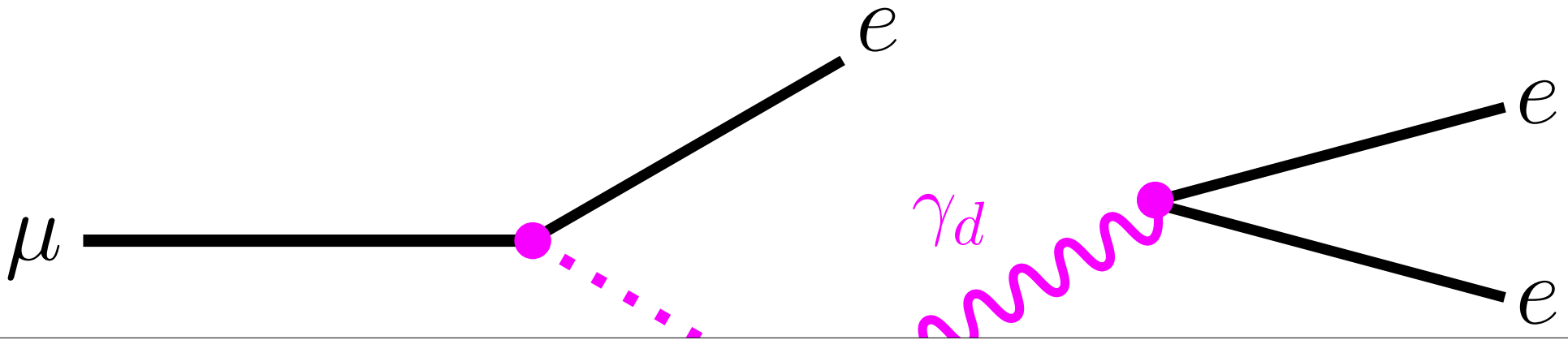
- Consider

$$\mathcal{L} \supset -y_{2ij}^{RL} \bar{u}_R^i$$

Match onto SM

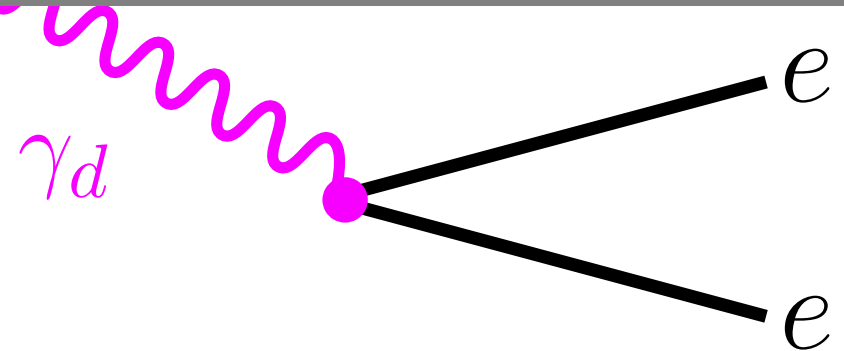
$C_{\tau\tau}$
 $C_{\tau\tau}$
 $C_{\tau\tau}$
 $C_{\tau\tau}$





Multi-electron muon decays

JHEP 10 (2023) 006, 2306.15631



Mu3e \rightarrow Mu5e

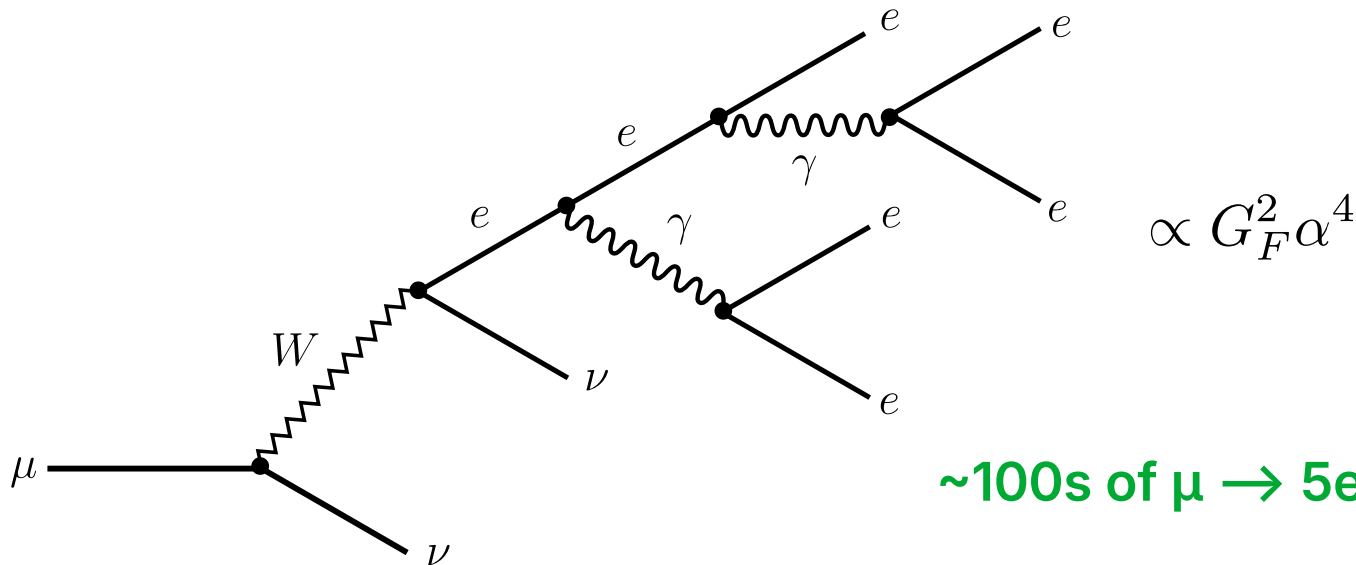
- **Mu3e will see $\sim 10^{15}$ total muon decays from the stopping target.**
- **With these statistics are there any other interesting channels?**
 - **What about $\mu \rightarrow 5e$?**

$\mu \rightarrow e e e e e \nu \nu$

- SM background for Mu5e

From MG5: $\mathcal{B}(\mu^+ \rightarrow e^+ e^- e^+ e^- e^+ \nu_e \bar{\nu}_\mu) = (3.929 \pm 0.001) \times 10^{-10}$

$$\mathcal{B}(\mu^+ \rightarrow e^+ e^- e^+ e^- e^+ \nu_e \bar{\nu}_\mu | \text{all } p_{e^\pm}^{\text{T,true}} > 10 \text{ MeV}) = (1.4 \pm 0.1) \times 10^{-14}$$



~100s of $\mu \rightarrow 5e\nu\nu$ events after cuts!

$\mu \rightarrow e e e e e$

- Higgsed $U(1)_D$ + SM portal via kinetic mixing

$$\mathcal{L}_{DS} = (D_\mu \phi)^\dagger D^\mu \phi - \frac{1}{4} F_d^{\mu\nu} F_{d\mu\nu} - \frac{\varepsilon}{2} F_d^{\mu\nu} F_{\mu\nu} - \mu^2 (\phi^\dagger \phi) - \lambda (\phi^\dagger \phi)^2$$

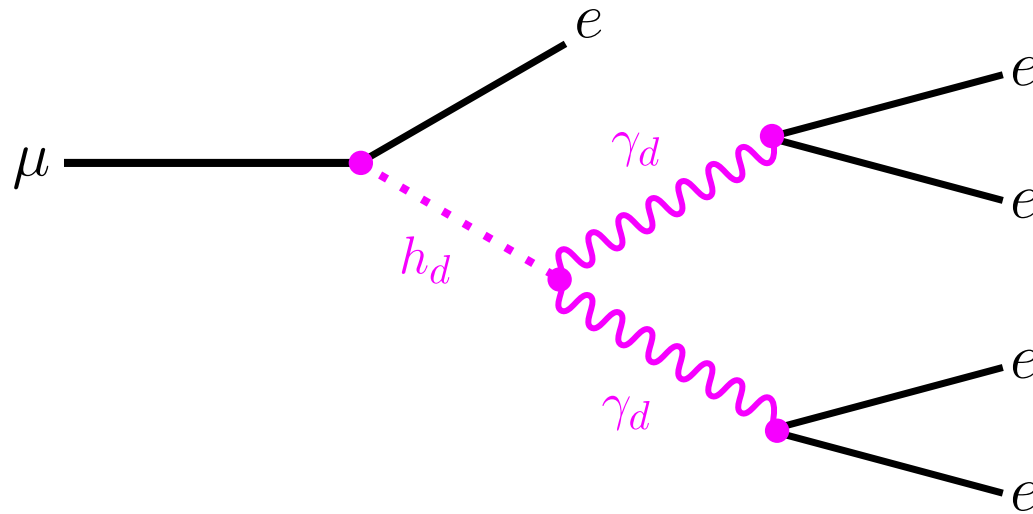
$$\mathcal{L}_{LFV} = -\frac{C_{ij}}{\Lambda} \phi (\bar{L}_i H) \ell_j + \text{h.c.}$$

$$\downarrow \quad y_{ij} \simeq \frac{Cv}{\Lambda}$$

$$\mathcal{L} \supset -m_{\ell_i} \bar{\ell}_{Li} \ell_{Ri} \left(1 + \frac{h}{v}\right) - y_{ij} \bar{\ell}_{Li} \ell_{Rj} h_d \left(1 + \frac{h}{v}\right) + \text{h.c.},$$

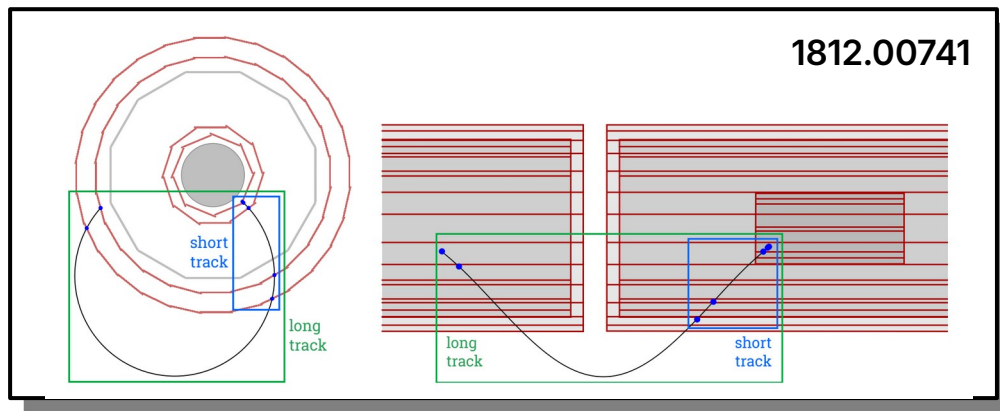
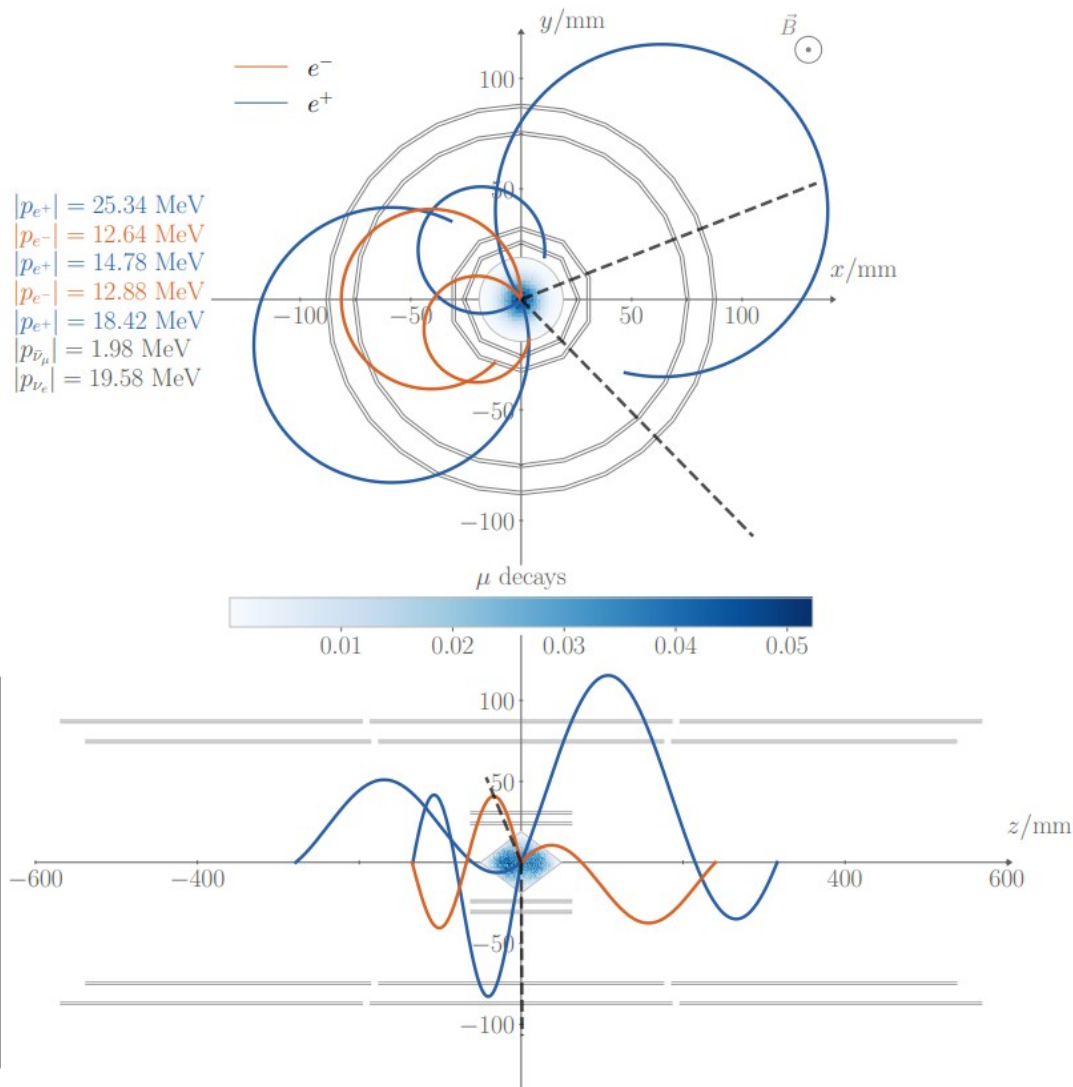
$$\mu \rightarrow e e e e e e$$

- Leads to cascade decay

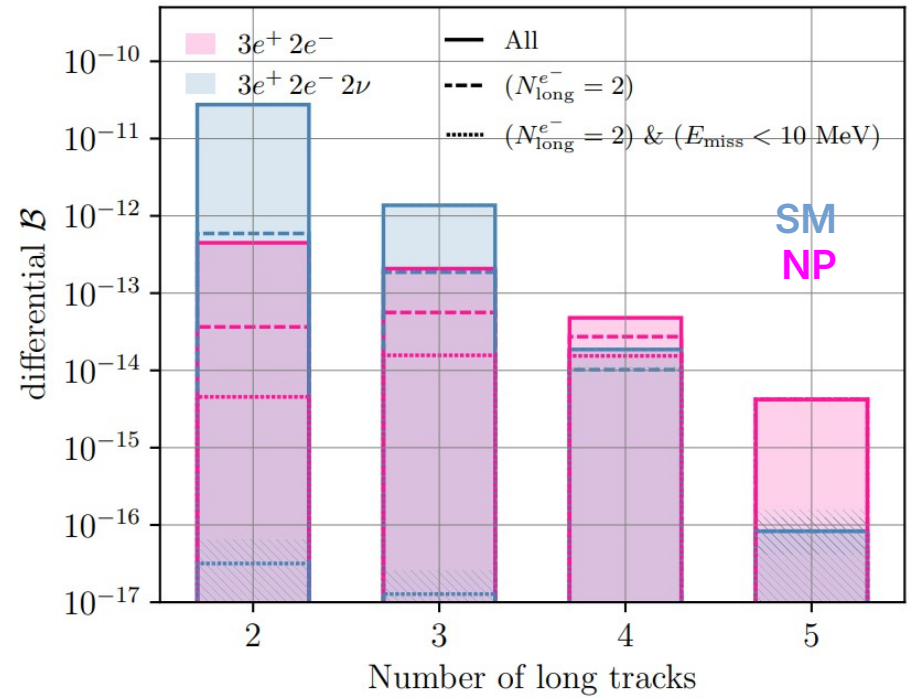
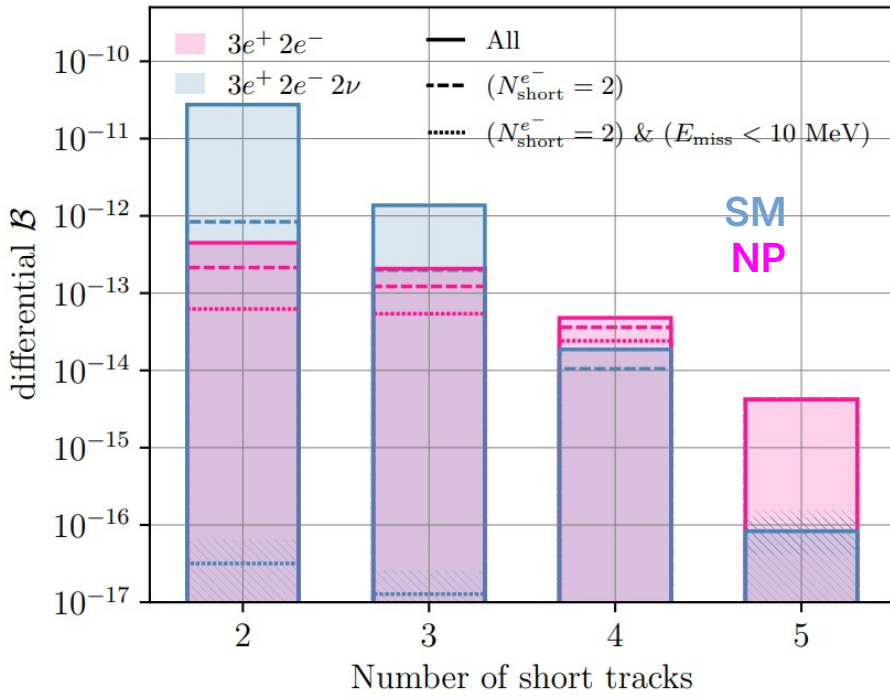


Signatures

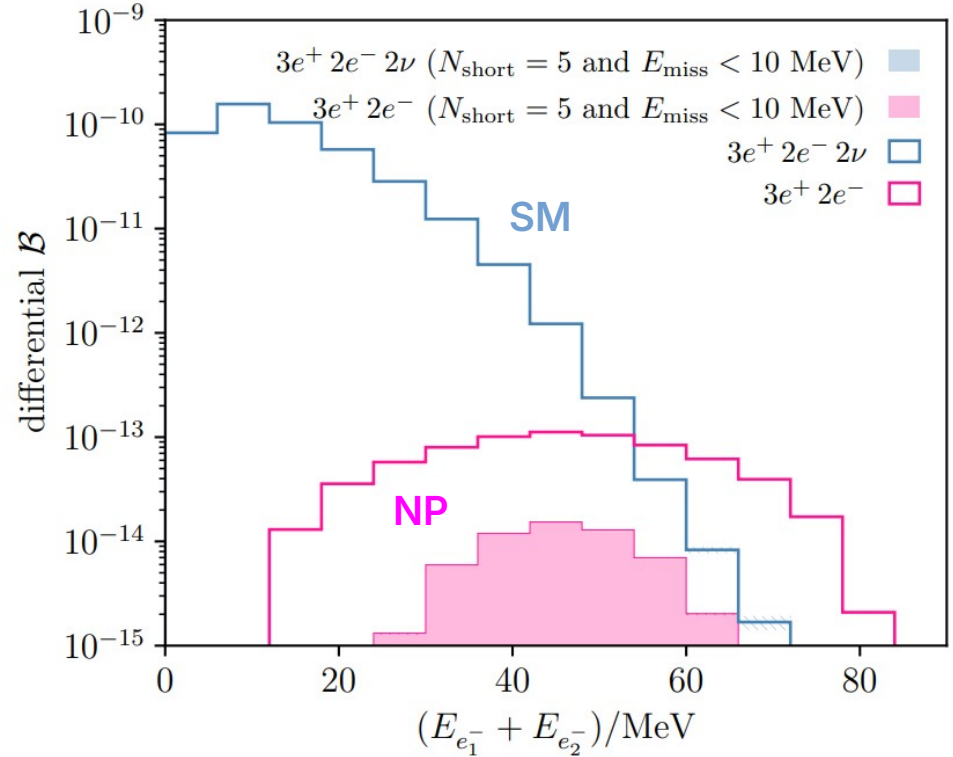
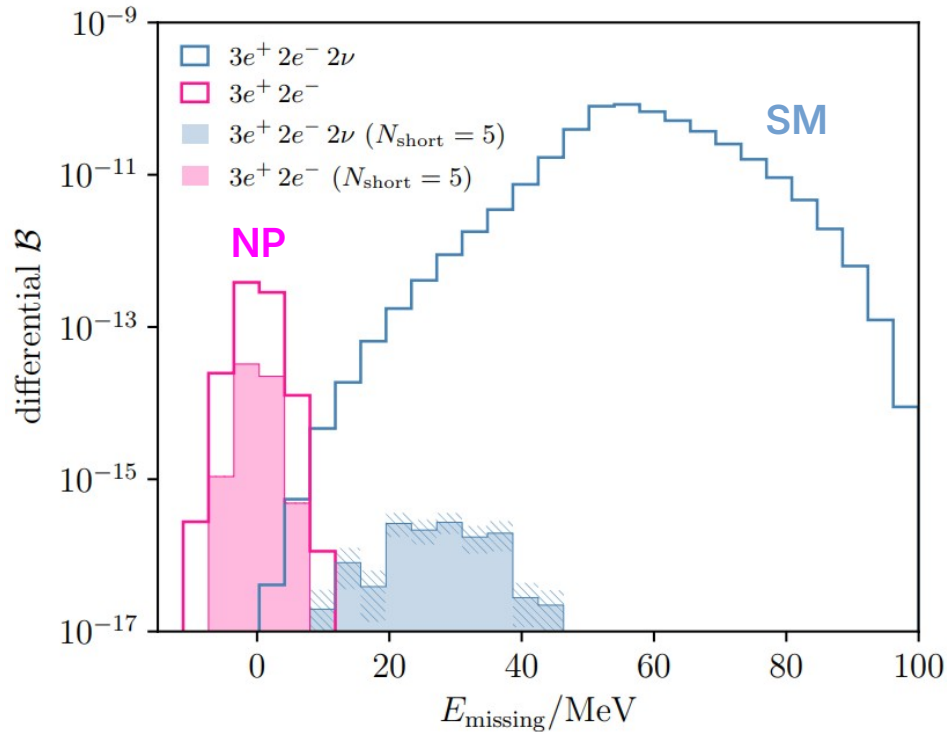
- Momentum of tracks must be reconstructed from energy deposits or 'hits' in the layers of the detectors.
- 4 hits = short track
- 6+ hits = long track



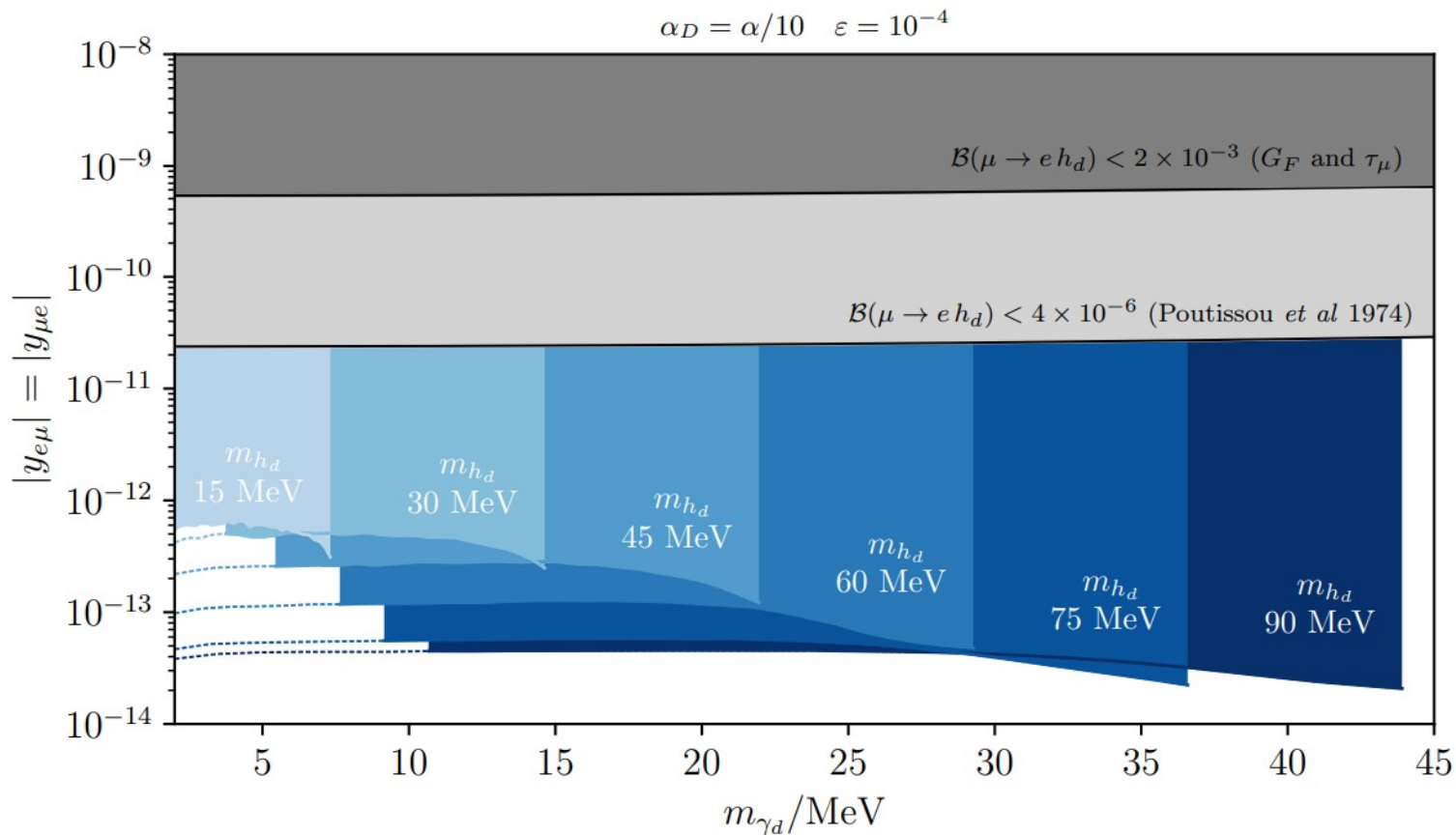
Signatures



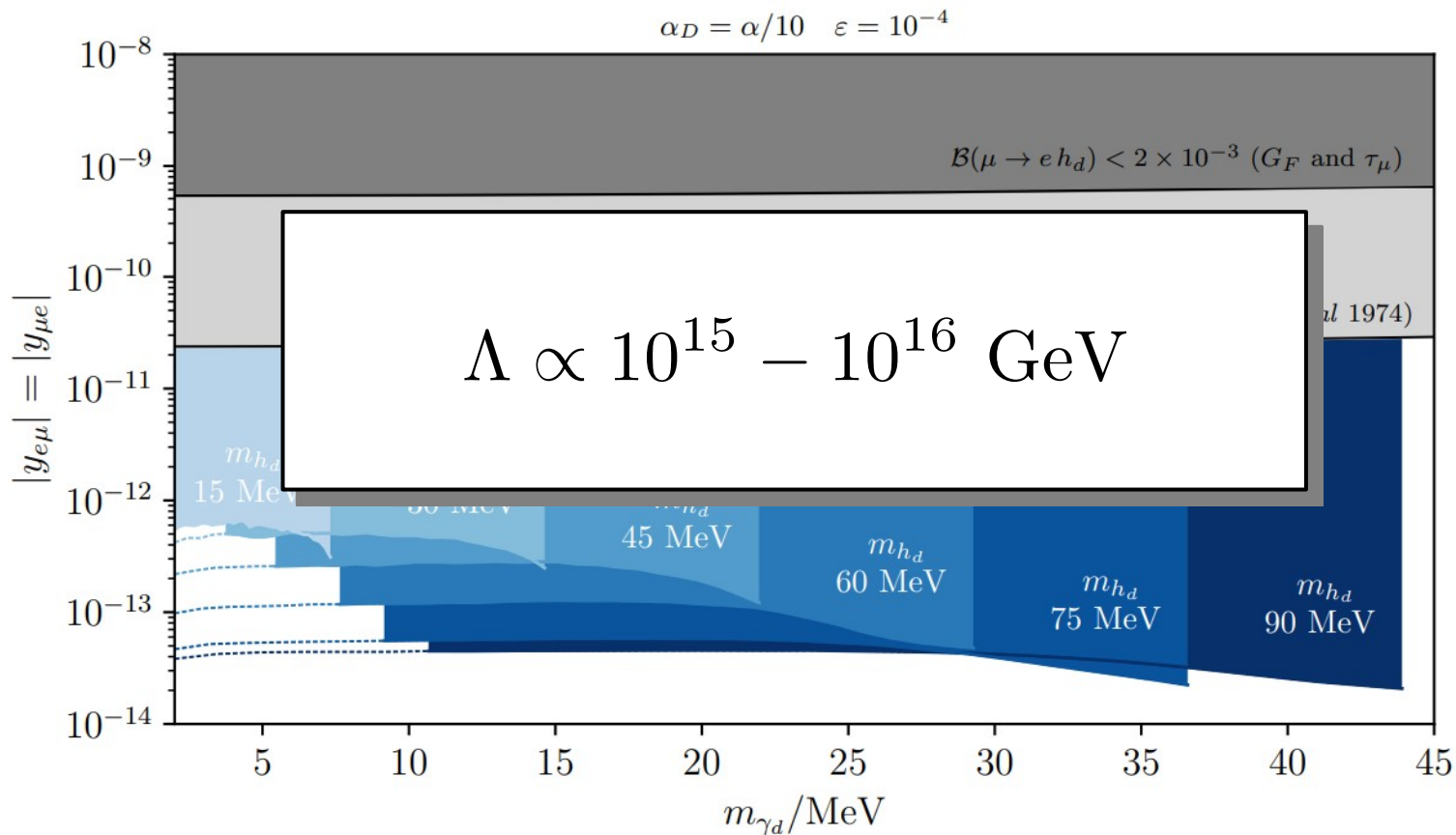
Signatures

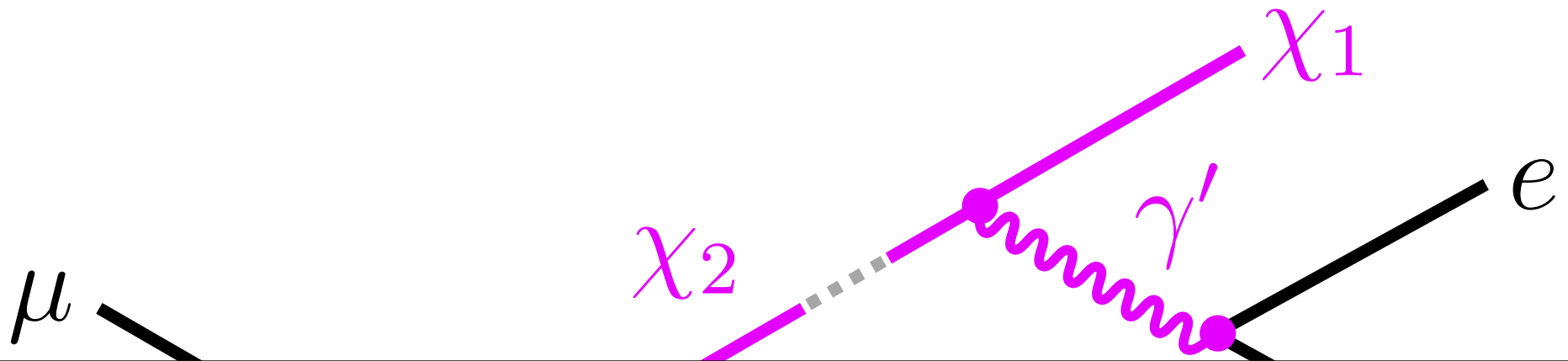


Reach

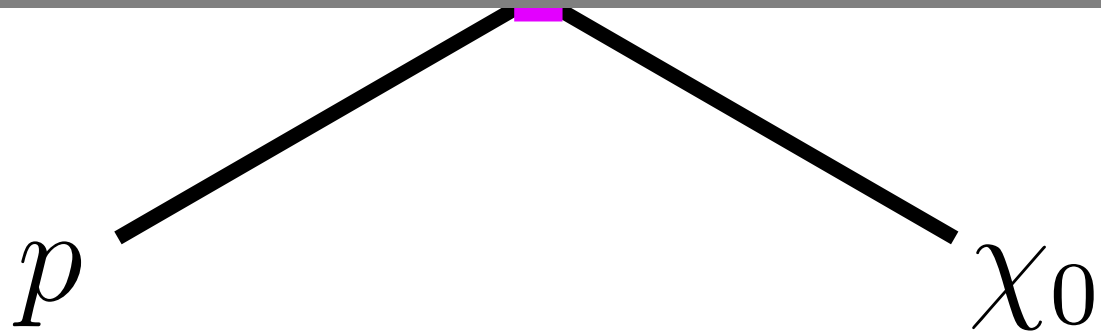


Reach





Muon-induced baryon number violation



2407.03450

Widening the view

- Can the CLFV signal @ Mu2e stem from non-CLFV physics?
- NP scenarios where $E_e > 105$ MeV?
 - Can we take advantage of the huge energy reservoir that is the nucleus?



- Three dark states + $U(1)_D$ + SM portal via kinetic mixing

$$\mathcal{L}_{\mu p} = G_{\mu p} (\bar{p} \chi_2) (\bar{\mu} \chi_0) + \text{h.c.}$$

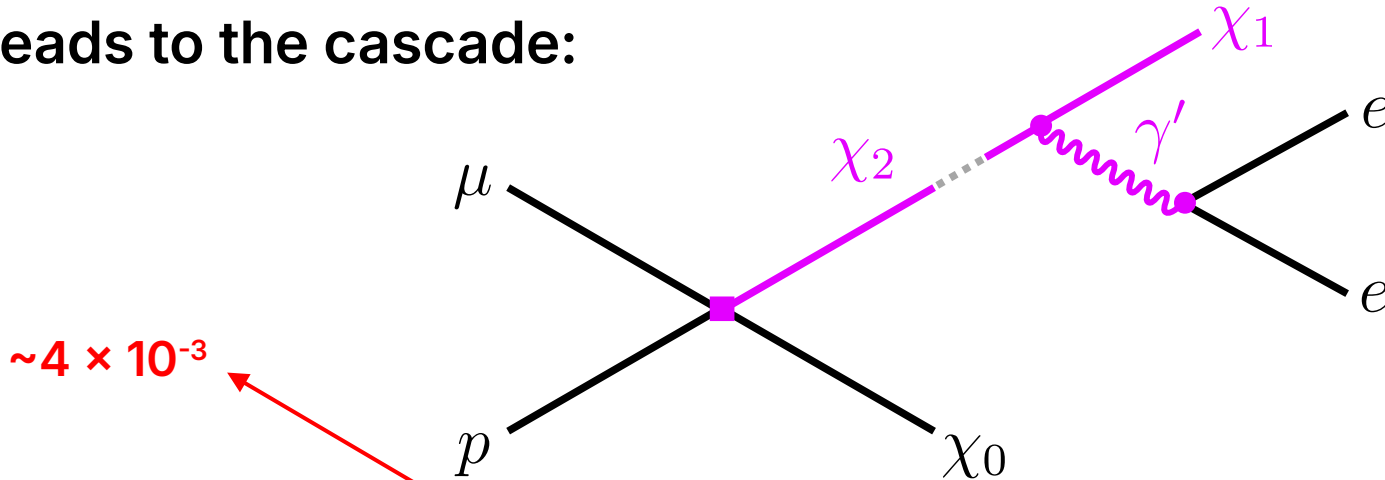
$$\mathcal{L}_{eA'} = e \varepsilon A'_\mu J_{\text{EM}}^\mu$$

$$\mathcal{L}_\chi = g_D (\bar{\chi}_2 \gamma^\mu \chi_1) A'_\mu + \text{h.c.}$$

$\mu \text{ } ^{27}\text{Al} \rightarrow \text{}^{26}\text{Mg}^{(*)} \chi_0 \chi_1 e e$

Benchmark: $m_2 = 1030 \text{ MeV}$, $m_1 = 900 \text{ MeV}$, $m_0 = 0$, $m_{A'} = 20 \text{ MeV}$,
 $G_{\mu p} = (300 \text{ TeV})^{-2}$, $\varepsilon = 10^{-4}$, $\alpha_D = 10^{-3}$

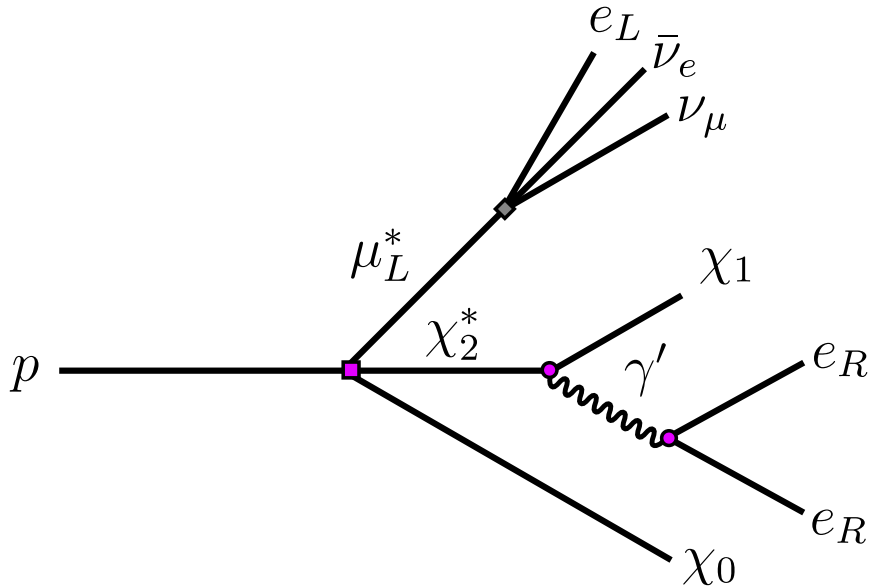
- Leads to the cascade:



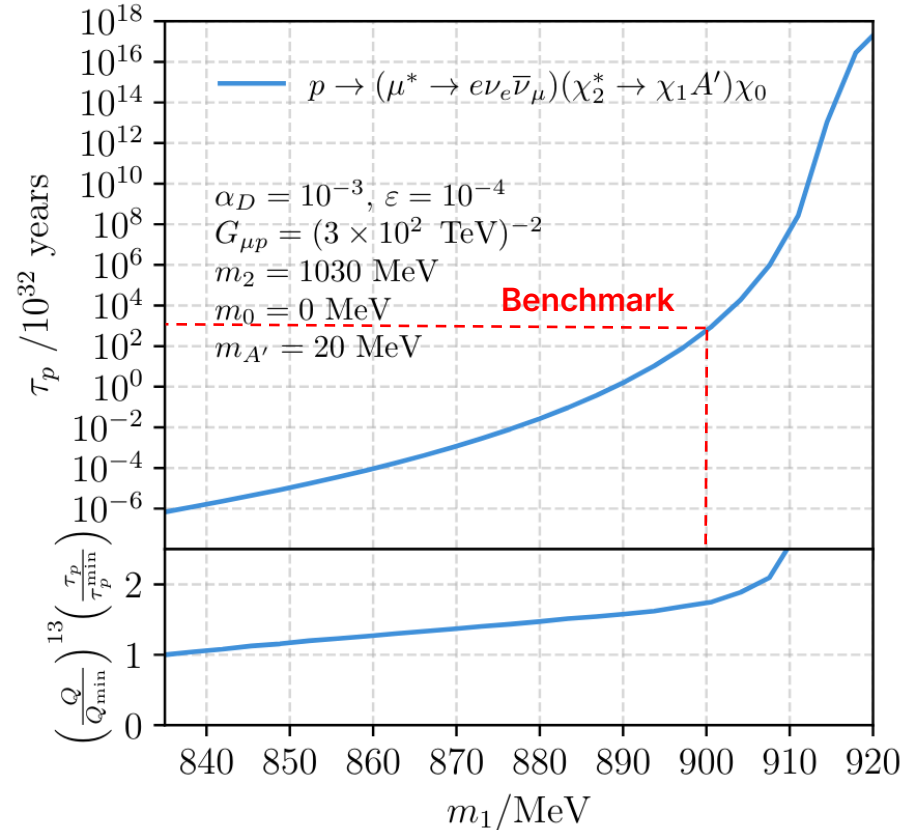
$\sim 4 \times 10^{-3}$

$$\Gamma(\mu \text{}^{27}\text{Al} \rightarrow \chi_0 \chi_2 \text{}^{26}\text{Mg}) \simeq r_{\text{p.s.}} \frac{G_{\mu p}^2}{G_F^2} \Gamma(\mu \text{}^{27}\text{Al} \rightarrow \nu_\mu n \text{}^{26}\text{Mg}) \longrightarrow R \equiv \frac{\Gamma_{\text{exotic}}}{\Gamma_{\mu\text{Al}}} \sim 10^{-15}$$

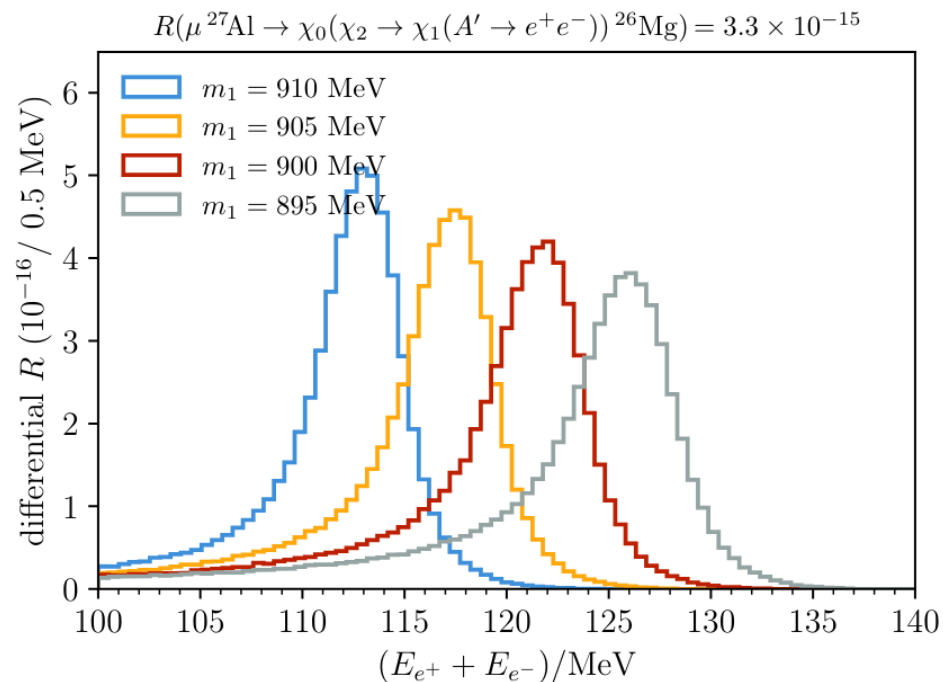
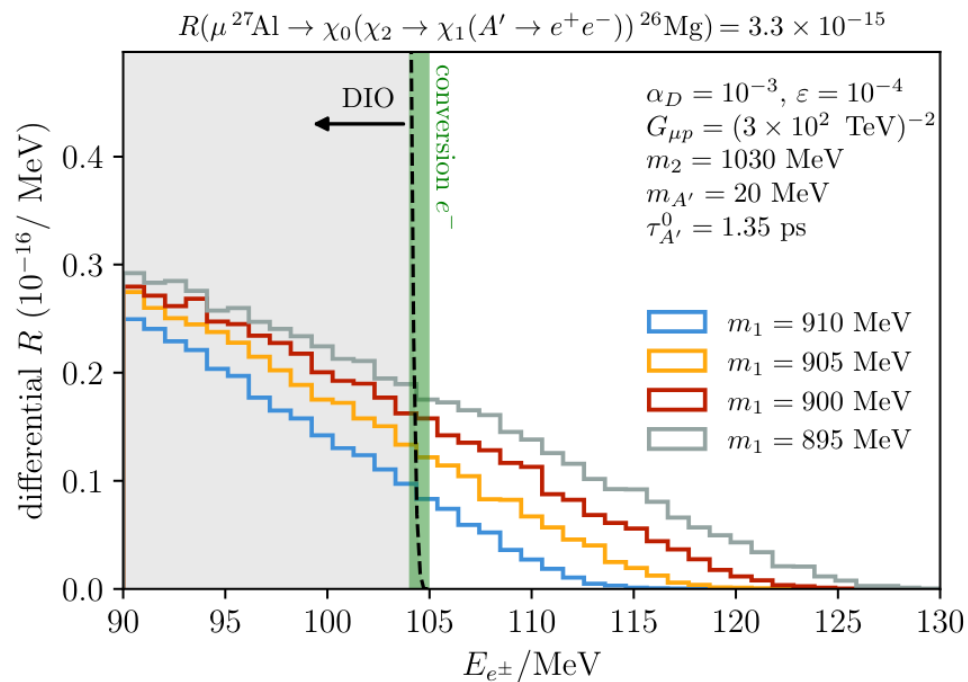
Tug-of-war with nucleon decay



$$\Gamma_p \propto \frac{G_{\mu p}^2 G_F^2 \alpha_D Q^{13}}{(16\pi^2)^4 m_\mu^2 m_2^2}$$



Signature



A UV completion

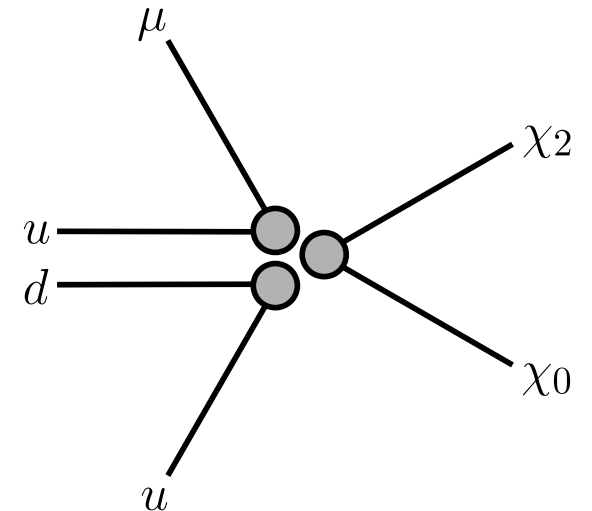
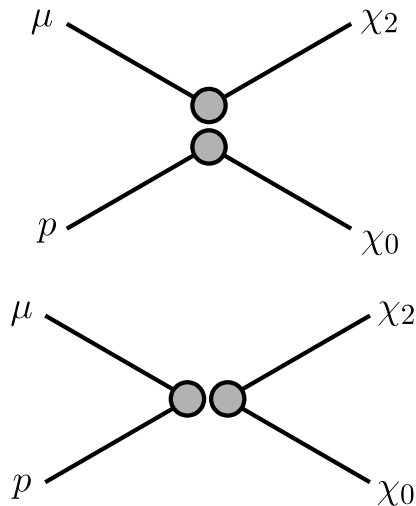
$$\mathcal{L}_{\mu p} = G_{\mu p} (\bar{p}\chi_2)(\bar{\mu}\chi_0) + \text{h.c.}$$

- What's the new physics reach? Naively:

$$G_{\mu p} \simeq 10^{-8} G_F \rightarrow \Lambda \simeq 10^3 \text{ TeV}$$

but Λ isn't fundamental...

$$\frac{1}{\Lambda^2} \simeq \frac{\Lambda_{\text{QCD}}^3}{\Lambda_{\text{col.}}^{d_{\text{col.}}} \Lambda_{\text{sing.}}^{5-d_{\text{col.}}}}$$

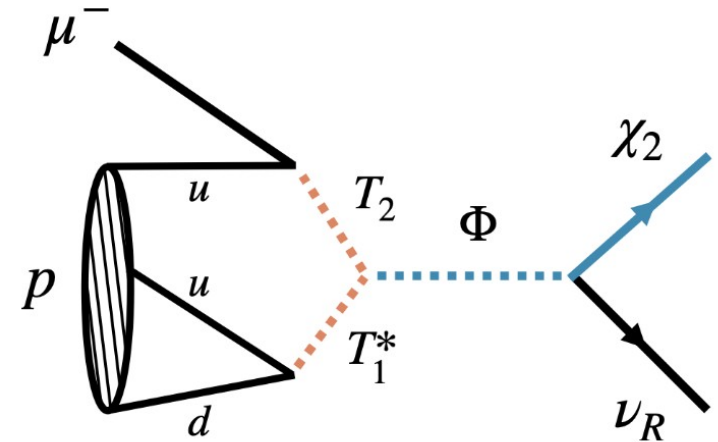


A UV completion

Introduce two colored scalars - a diquark T_1 and a leptoquark T_2 as well as a complex scalar Φ .

$$\mathcal{L} \supset -y_{ud}(\overline{u_R^i} d_R^j)\epsilon_{ijk}T_1^k - y_{\mu u}(\overline{u_R^i} \mu_R)(T_2^*)_i + \text{h.c.}$$

$$\mathcal{L} \supset \rho T_1^{k*} T_{2k} \Phi^* + y_\chi \Phi(\overline{\nu_R} \chi_{2R}^C) + \text{h.c.}$$



A UV completion

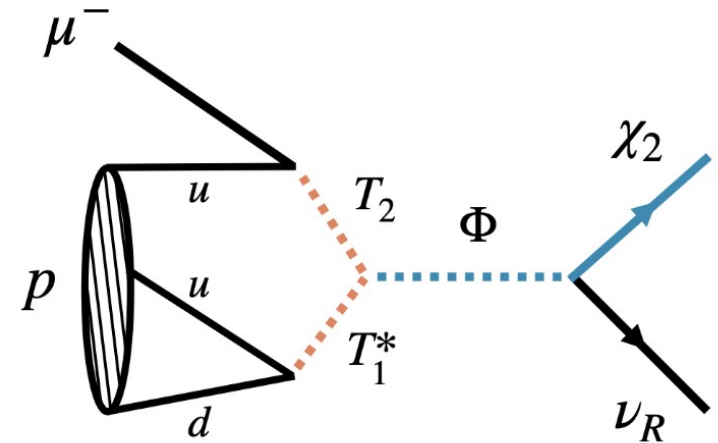
Introduce two colored scalars - a diquark T_1 and a leptoquark T_2 as well as a complex scalar Φ .

Integrate out T_1 and T_2 , for off-shell Φ :

$$\mathcal{L}_{\text{eff}} = \frac{1}{\Lambda_{\text{col}}^3} \frac{1}{\Lambda_{\text{sin}}^2} (\overline{u_R^{iC}} \mu_R) \epsilon_{ijk} (\overline{u_R^{jC}} d_R^k) (\overline{\nu_R} \chi_{2R}^C) + \text{h.c.}$$

$$\frac{1}{\Lambda_{\text{col}}^3} = y_{ud} y_{\mu u} \frac{\rho}{m_{T_1}^2 m_{T_2}^2}$$

$$\frac{1}{\Lambda_{\text{sin}}^2} = \frac{y_\chi}{m_\Phi^2}$$



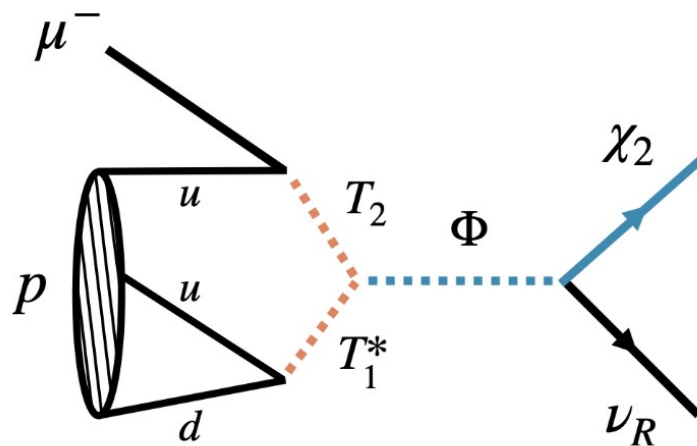
A UV completion

Introduce two colored scalars - a diquark T_1 and a leptoquark T_2 as well as a complex scalar Φ .

Integrate out T_1 and T_2 , for off-shell Φ :

$$\tilde{G}_{\mu p} \simeq 10^{-6} G_F$$

$$\sim 10^{-6} G_F y_{ud} y_{\mu u} y_\chi \left(\frac{1 \text{ TeV}}{\sqrt{m_{T_1} m_{T_2}}} \right)^4 \left(\frac{\rho}{4 \text{ TeV}} \right) \left(\frac{2 \text{ GeV}}{m_\Phi} \right)^2$$



A UV completion

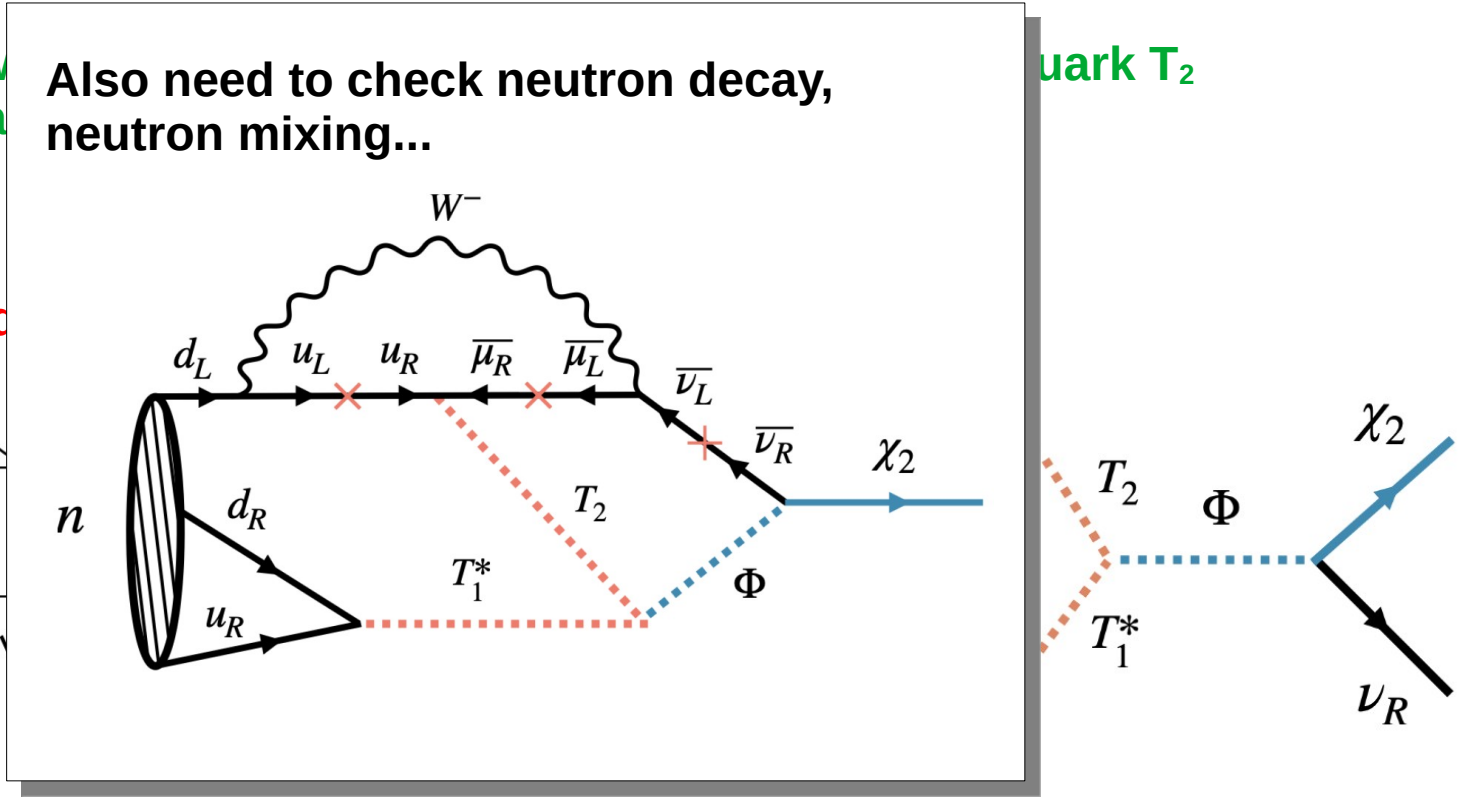
Introduce two new particles
as well as a new interaction

Integrate out T_1 and T_2

Also need to check neutron decay,
neutron mixing...

quark T_2

$$\tilde{G}_{\mu p} \supseteq \sim 10^{-6} G_F y_{ud} y_{\mu u} y_\chi \left(\dots \right)$$



Conclusions

- **New EFT tower for model building in $N\mu \rightarrow Ne$**
 - Consistent nuclear EFT with all allowed nuclear responses
 - Rate can be computed easily using the MuonBridge software suite
- **Mu3e should be able to see ~ 100 s of $\mu \rightarrow eeeee\nu$ events and can be very constraining on NP models** (for the described model).
- **We hope Mu3e adds the $\mu \rightarrow eeeee$ channel to their analysis pipeline**
- **Interesting non-CLFV physics at Mu2e (and COMET)**
- **We hope Mu2e + COMET add highly energetic electrons (above the conversion energy) to their analysis pipeline**

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Thank you :)